

1st Law $\Sigma \vec{F} = 0 \Leftrightarrow \vec{a} = 0$

$\Leftrightarrow (\vec{v} = 0)$ static equilibrium
OR

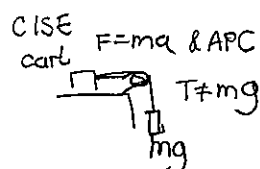
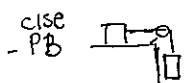
$\vec{v} = \text{constant}$ dynamic equilibrium
speed & dir, straight line

- Law of Inertia - stubbornness
- resistance to change in motion
- property of matter

• mass is a measure of inertia

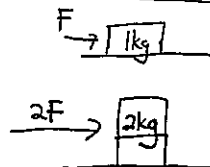
CISE: 1kg, elephant

- next time questions
- Burt equilibrium
- plane
- gymnast 1kg $\rightarrow$ 10N $w = mg$



2nd Law $\Sigma \vec{F} = m \vec{a}$

1N = 1kg/m/s²



$\vec{a} = \frac{\vec{F}}{m}$

ex3

car 1500kg

avg force to stop it from 100km/h in 55m?

$\leftarrow a$
1500kg $\rightarrow$ 100km/h $\rightarrow$ 100000m / 3600s = 250/9 m/s = 27.8 m/s

$\leftarrow F$ (friction)

$a \Rightarrow F$

$v_f^2 = v_0^2 + 2a\Delta x$

$0 = \left(\frac{250}{9} \frac{m}{s}\right)^2 + 2a(55m)$

$a = -7.01 \text{ m/s}^2$

$\Sigma F = ma = 1500kg \cdot -7.01 \text{ m/s}^2 = -1.1 \times 10^4 \text{ N}$

3rd Law $\vec{F}_{H \text{ on } T} = -\vec{F}_{T \text{ on } H}$

- every action has an equal and opposite reaction
- always on different objects. Don't cancel out!

* see APC block & mason example

* about tension

- CISE { apple-earth, pull same
horse-cart don't cancel
tension - Tarzan/horse
spring scale

ch3

4.6

Vocab

Weight

Support / normal force, apparent weight
(spring scale reading)
tension

Question
measures?



4.7

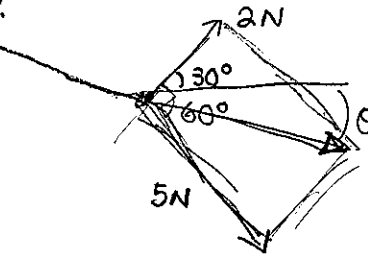
Free-body diagrams

• translational motion, consider ^{as} point particle

ex9

Use spring scales to show $\vec{F}$ vector addition works!

Try it!



$$\Sigma \vec{F} = \langle 2\cos 30^\circ + 5\cos 60^\circ, 2\sin 30^\circ + 5\sin 60^\circ \rangle$$

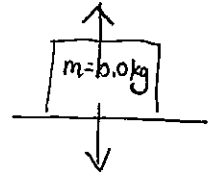
$$= \langle \sqrt{3} + \frac{5}{2}, 1 - \frac{5\sqrt{3}}{2} \rangle$$

$$= \langle 4.23, -3.33 \rangle$$

$$F = \sqrt{28.98} \text{ N} = 5.38 \text{ N}$$

$$\theta = 38^\circ$$

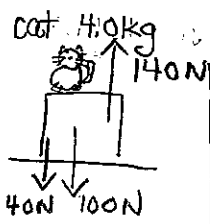
ex6



$$w = ? \quad 100 \text{ N}$$

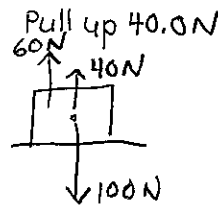
$$n = ? \quad 100 \text{ N}$$

$$g = 10 \text{ m/s}^2$$



$$w = 100 \text{ N}$$

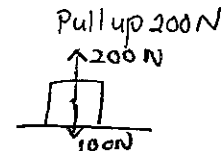
$$n = 140 \text{ N}$$



$$w = 100 \text{ N}$$

$$n = 60 \text{ N}$$

(ex7)



What happens?

$$\Sigma F = 100 \text{ N}$$

$$a = \frac{\Sigma F}{m} = 10 \text{ m/s}^2 \text{ upward}$$

ex8

Apparent weight

See APC Ch3 P1b cat in elevator

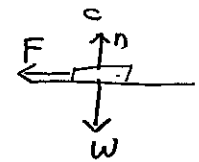
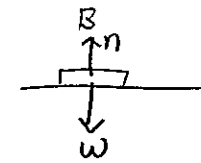
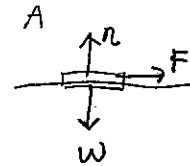
ex10

Hockey Puck on ice

Correct free-body diagram?

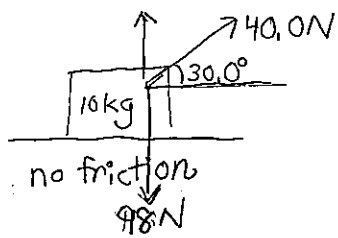
const. speed: B

slowing down: C



• Problem-solve: 1) free body 2) $\Sigma F = ma$ & kinematic 3) x & y separately

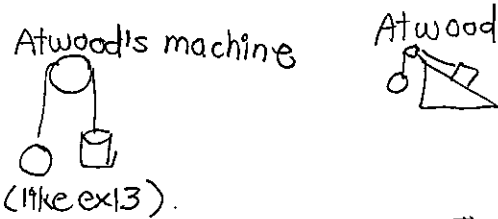
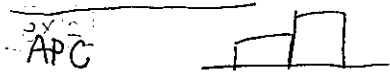
ex11



a) $\vec{a}$? b) $\vec{n}$? c) If pull harder, $\vec{n}$ will be same?

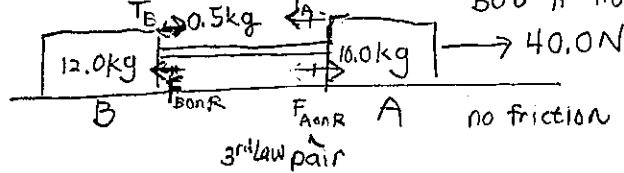
a) $\Sigma F_y = 0$
 $\Sigma F_x = ma_x$
 $a_x = \frac{40 \cos 30^\circ}{10 \text{ kg}} = 3.46 \text{ m/s}^2$

b) $40 \sin 30^\circ + n = 98$
 $n = 98 - 40 \sin 30^\circ = 78.0 \text{ N}$



ex12

rope in equilibrium? No! (so if $m \neq 0$, $a \neq 0$, $T_{\text{right}} \neq T_{\text{left}}$)
 But if $m=0$, $\Sigma F=0$



a) a_A ? a_B ? b) T_{right} ? T_{left} ?
 same

$\Sigma F = ma$

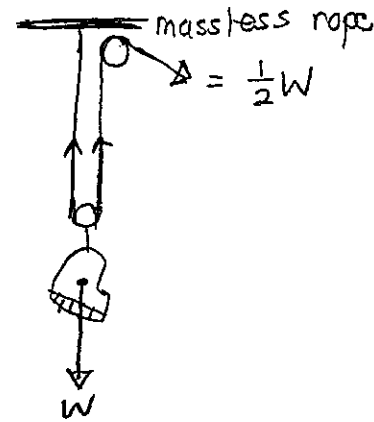
$a = \frac{40}{22.5} = 1.78 \text{ m/s}^2$

$T_A - F_{B \text{ on } R} = (0.5 \text{ kg})(1.78 \text{ m/s}^2)$
 0.84 check OK 0.89

$F_{B \text{ on } R} = T_B = m_B a_B = 21.3 \text{ N}$
 $40 - T_A = m_A a_A \Rightarrow T_A = 22.2 \text{ N}$
 17.8

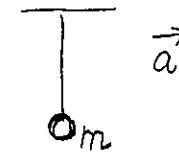
ex14

Pulley: less force, more distance
 See CISE animated



ex15

Accelerometer



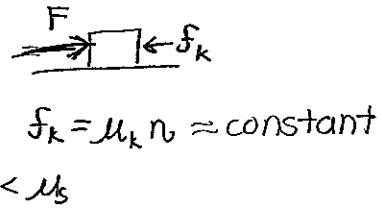
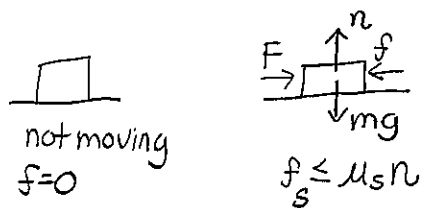
$\Theta = ?$
 a) when car $a = 1.20 \text{ m/s}^2$
 b) when constant $v = 90 \text{ km/h}$
 ($\Sigma F = 0 \Rightarrow \Theta = 0$)



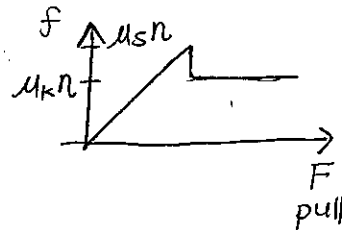
$\Sigma F_y = 0$
 $T \cos \Theta = mg$

a) $\Sigma F_x = ma$
 (left by inertia, $T \sin \Theta$ is the pull that makes it move right with car)
 $T \sin \Theta = ma$
 $\frac{mg}{\cos \Theta} \sin \Theta = ma$
 $\tan \Theta = \frac{a}{g}$
 $\Theta = \tan^{-1} \left(\frac{a}{g} \right)$
 $= 7.0^\circ$

4.8 Friction & Inclines

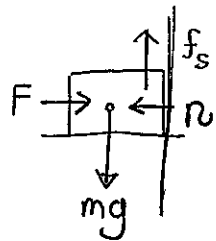


wood on wood	μ_s 0.4	μ_k 0.2
ice on ice	0.1	0.03
rubber-dry concrete	1.0	0.8
joints in limbs	0.01	0.01



ex 17 $\mu_s = ?$, $m = 10.0 \text{ kg}$

Press box to wall with how much ^{200N} force to keep from slipping. $\mu_s \geq ?$



$$f_s = mg$$

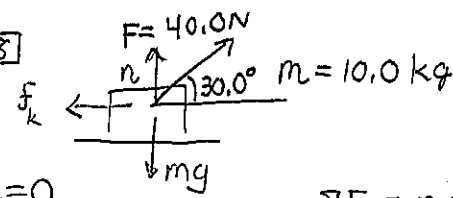
$$f_s \leq \mu_s n$$

$$\mu_s \geq \frac{mg}{n}$$

(but: $F \uparrow n \uparrow f_s \uparrow ??$)
No
 $f_s \leq \mu_s n$
NOT equal

$$\frac{100 \text{ N}}{200 \text{ N}} = 0.5$$

ex 18



$\mu_k = 0.30$
 $a = ?$

$$\Sigma F_y = 0$$

$$n + F \sin \theta = mg$$

$$\Sigma F_x = ma$$

$$F \cos \theta - \underbrace{f_k}_{\mu_k n} = ma$$

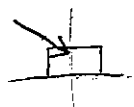
$$a = \frac{F \cos \theta - \mu_k (mg - F \sin \theta)}{m}$$

$$= \frac{40 \cos 30^\circ - 0.3 (10 \times 9.8 - 40 \sin 30^\circ)}{10}$$

$$= \boxed{1.1 \text{ m/s}^2}$$

Bonus: constant velocity a) F in terms of weight, μ_k , θ
b) θ for $F_{\min}$?

ex19 Push or pull a sled?



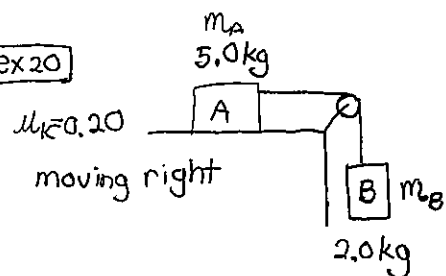
increases n ,
friction

$\Rightarrow F \uparrow$ to accelerate
or maintain speed



$$n \downarrow \Rightarrow f_k \downarrow \Rightarrow F \downarrow$$

ex20



$$T = ?$$

$$a = ?$$

$$\Sigma F = ma$$

$$m_B g - \mu_k (m_A g) = (m_A + m_B) a$$

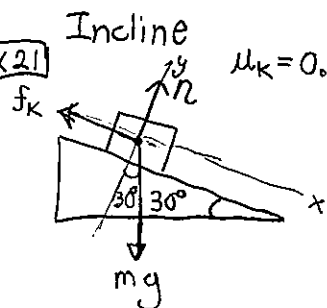
$$\Rightarrow a = 1.4 \text{ m/s}^2$$

$$m_B g - T = m_B a$$

$$\Rightarrow T = 17 \text{ N}$$

OR $T - m_A g \mu_k = m_A a$

ex21



$\mu_k = 0.10$ sliding down

$$a = ?$$

$$\Sigma F_y = 0$$

$$n = mg \cos \theta$$

$$\Sigma F_x = ma$$

$$mg \sin \theta - \mu_k (mg \cos \theta) = ma$$

$$a = g (\sin \theta - \mu_k \cos \theta)$$

$$= 9.8 \left(\frac{1}{2} - 0.1 \frac{\sqrt{3}}{2} \right)$$

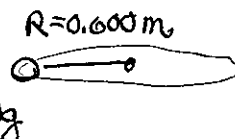
$$= 4.1 \text{ m/s}^2$$

Ch5

Giancoli

Already described 5-1
in ch 3 vectors 5-4 $\frac{v^2}{r}$ proof

ex1



2.00 rev/second

$$a_c = ? \frac{v^2}{R} = \left(\frac{2 \times 2\pi \times 0.6}{1 \text{ s}} \right)^2 \frac{1}{0.6}$$

$$= 94.7 \text{ m/s}^2 \quad (\text{m doesn't matter})$$

- Is there an outward force? No! (inertia)
- It's ΣF to center that makes the curve

ex3

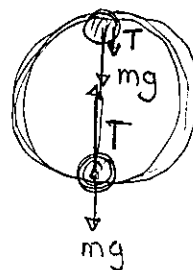
$$T = m a_c = 0.15 \times 94.7 = 14.2 \text{ N}$$

to center

Vertical Circles

ex4

Ball on string. m, R



a) $v_{\min}$ to continue in arc? b) $T_{\text{bottom}}?$

$$\Sigma F_R = mg = m \frac{v^2}{R}$$

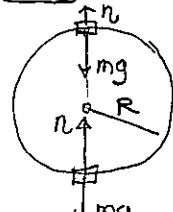
$$v_{\min} = \sqrt{gR}$$

$$T - mg = m \frac{v^2}{R}$$

$$T = m \left(g + \frac{v^2}{R} \right)$$

ex5

Ferris wheel R given



a) $n_{\text{top}}?$

c) $v_{\max}$ to prevent flying off?

b) n at bottom?

$$a) \quad mg - n = m \frac{v^2}{R}$$

$$b) \quad n - mg = m \frac{v^2}{R}$$

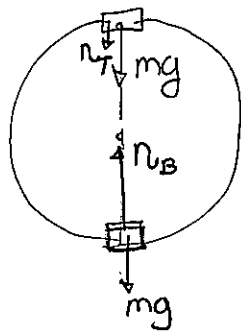
$$n_T = m \left(g - \frac{v^2}{R} \right)$$

$$n_B = m \left(g + \frac{v^2}{R} \right)$$

$$c) \quad v_{\max} = \sqrt{Rg}$$

$\Rightarrow$ negative a (centrifugal to hold down)

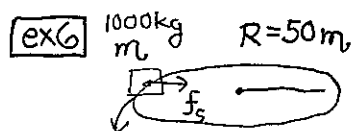
② Loop-the-loop rollercoaster



a) n_T b) n_B

c) $v_{\min}$ to keep from falling out?
(same as tension example)

5-3 (Banked) Curves



$v = 15 \text{ m/s}$
constant

$$\Sigma F_r = m a_r$$

$$\mu_s mg = m \frac{v^2}{r}$$

max force possible

$$\mu_s \geq \frac{v^2}{rg} = \frac{15^2}{50 \times 9.8} = 0.459$$

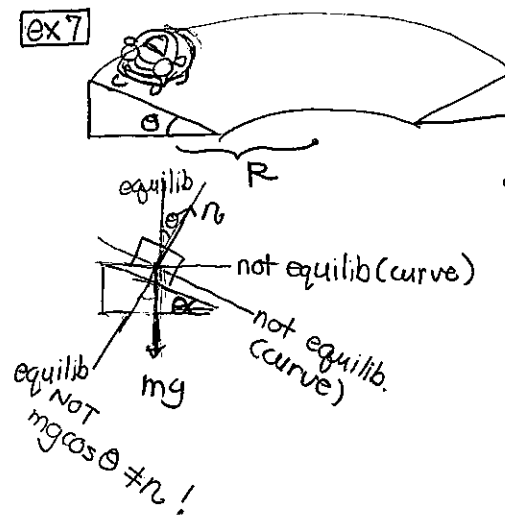
Will it skid?

a) $\mu_s = 0.60$ (dry pavement)
b) $\mu_s = 0.25$ (icy)

a) No

b) yes

ex7



Banked Curve

No friction needed
($\vec{n}$ pushes radially)

Find θ for constant v , R

$$\Sigma F_n = 0$$

$$\Sigma F_r = m \frac{v^2}{R}$$

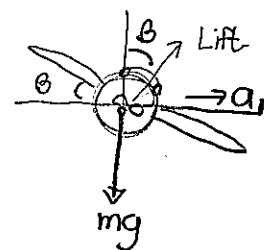
$$mg = n \cos \theta$$

$$n \sin \theta = m \frac{v^2}{R}$$

$$\rightarrow mg \tan \theta = m \frac{v^2}{R}$$

$$\theta = \tan^{-1} \left(\frac{v^2}{gR} \right)$$

Banked Curves in Airplanes - see APC



Lift makes it curve $\vec{a}_c$. Q) when $\beta = 84^\circ$, black out?

pilot's apparent weight

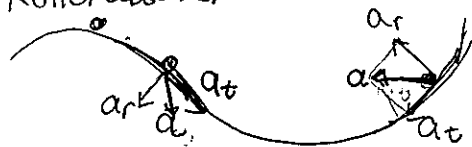
$$L \cos \beta = mg$$

$$n = L = \frac{mg}{\cos \beta} = 9.6 mg \text{ yes}$$

heart can't pump blood to brain

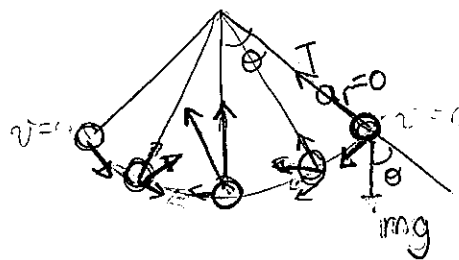
5-4 Nonuniform Circular Motion

Rollercoaster



$$\vec{a} = \vec{a}_t + \vec{a}_r$$

Pendulum Bonus in Test 1

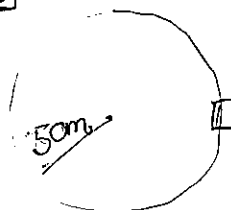


$$\vec{a} \neq m\vec{g}$$

$$\vec{a} = \vec{a}_t$$

equilibrium (no component of $\vec{a}$ in that dir) $\Rightarrow T = mg \cos \theta$

ex8



0 ~ 15 m/s in 5s

- $a_t = ?$
- $a_r = ?$ when $v = 15 \text{ m/s}$
- $a = ?$ when $v = 15 \text{ m/s}$

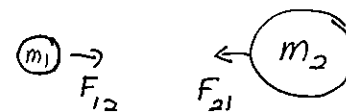
$$a_t = \frac{15 \text{ m/s}}{5 \text{ s}} = 3.0 \text{ m/s}^2$$

$$a_r = \frac{15^2}{50} = 4.5 \text{ m/s}^2$$

$$\Rightarrow a = \sqrt{9 + 4.5^2} = \boxed{5.4 \text{ m/s}^2}$$

5-3 Newton's Universal Law of Gravitation

$$\vec{F}_g = -G \frac{m_1 m_2}{r^2} \hat{r}$$



equal & opposite. Attractive.

$$G = 6.67 \times 10^{-11} \frac{\text{Nm}^2}{\text{kg}^2}$$

inverse square law

for uniform sphere, same as if all mass at CM

Cavendish experiment found G

HW Bonus (Read book)

- (B1) How did Newton figure out $F_g \sim \frac{1}{r^2}$?
Show calculations

ch5 (ex4) Moon goes around Earth every $T = 27.3 \text{ days}$

Earth Moon distance
1.48 $R_{EM} = 384,000 \text{ km}$

(Hipparchus lunar eclipse? parallax?)
(B2) Trigonometry
- 1st Earth's circumference
(B3) Eratosthenes

$$a_c = \frac{v^2}{r} = \frac{\left(\frac{2\pi \times 3.84 \times 10^8 \text{ m}}{27.3 \times 24 \times 3600 \text{ s}} \right)^2}{3.84 \times 10^8}$$

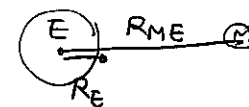
$$= 2.72 \times 10^{-3} \text{ m/s}^2$$

$$a_c = \frac{2.7 \times 10^{-3}}{9.8} g = \frac{1}{3600} g$$

$$\frac{R_E}{R_{EM}} = \frac{6380 \text{ km}}{384,000 \text{ km}} \approx \frac{1}{60}$$

$$R_{ME} = \frac{1}{60} R_E \Rightarrow \text{further, gravity drops by } \frac{1}{r^2}$$

$$F_M \sim \frac{1}{60^2} F_E \quad \therefore F_g \sim \frac{1}{r^2}$$



ⓑ How did Cavendish measure G (diagram)

ⓐ why is $g = 9.80 \text{ m/s}^2$? $g = G \frac{m_E}{R_E^2}$

b) How scientists figured out M_E (Cavendish was first once G was measured, R_E already known, g by dropping)

$$m_E = \frac{g R_E^2}{G} = \frac{9.80 \times (6.38 \times 10^6 \text{ m})^2}{6.67 \times 10^{-11}} \\ = 5.98 \times 10^{24} \text{ kg}$$

ex 9 Attraction between 50 kg & 70 kg on a bench

$$F_g = G \frac{m_1 m_2}{r^2} \approx 10^{-6} \text{ N}$$

$r \approx 0.5 \text{ m}$
(from CM, side by side)

$$\textcircled{a} g_{\text{moon}} = \frac{G \frac{M_M}{R_M^2}}{9.80} g_{\text{Earth}} \\ = \frac{1}{6} g_{\text{Earth}}$$

② CISE ch7

②

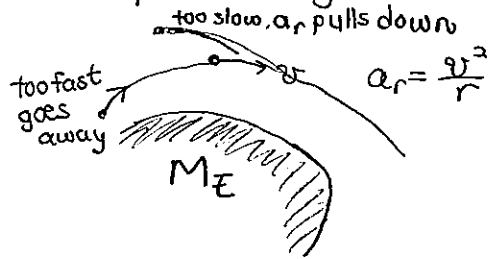
- Weight of Space shuttle on Earth is W (big)
- Weight in orbit 200 km above Earth? 94%

Space Shuttle orbits at 200 km above Earth's surface

a) Why are astronauts floating?

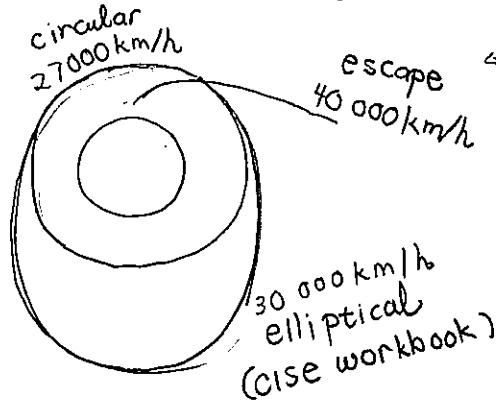
- Not 0 gravity. They're falling around the Earth.
- See CISE pictures. Speed is fast enough to match curvature.
- If $v = 0$, would drop down

(speed v by launch & inertia keeps it going)



b) Is the weight up there 0%? 100%? (94%)

Launch speed / angle? escape?



elliptical. How to calculate??

$$\% = \frac{\frac{M_E}{(r_E + h)^2}}{\frac{M_E}{r_E^2}} = \left(\frac{r_E}{r_E + h} \right)^2 = \left(\frac{6.38 \times 10^6}{6.38 \times 10^6 + 2 \times 10^5} \right)^2 = 0.94$$

ex12 Geosynchronous satellite

a) - only if... above equator

a) altitude?

b) speed of satellite?

$$F_g = G \frac{M_E m}{r^2}$$

c) compare to speed of satellite 200 km above Earth's surface
 $v \propto ? r$

$$a) \quad G \frac{M_E}{r^2} = \frac{v^2}{r} \quad \leftarrow \text{match Earth rotation}$$

$$G \frac{M_E}{R^2} = \left(\frac{2\pi R}{24 \times 3600 \text{ s}} \right)^2$$

$$R^3 = \frac{G M_E \left(\frac{24 \times 3600}{2\pi} \right)^2}{4\pi^2} \Rightarrow R = 4.22 \times 10^7 \text{ m}$$

$\uparrow$ $\uparrow$ $\uparrow$
 $R_E + h$ 6.67×10^{-11} 5.98×10^{24} $42,200,000$
 $h = R - R_E = 36,000 \text{ km}$ $(42,200 \text{ km})$

$$h = R - R_E = 36,000 \text{ km}$$

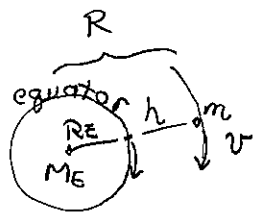
$$6.38 \times 10^6 = 6,380 \text{ km}$$

$$h_2 = 200 \text{ km}$$

$$v_{\text{geo}} = \frac{2\pi R}{T_{\text{day}}} \quad \text{OR} \quad \sqrt{\frac{G M_E}{R}} = 3070 \text{ m/s}$$

$$c) \quad v = \sqrt{\frac{G M_E}{R_E + 2 \times 10^5}} \quad \text{OR} \quad v \sim \sqrt{\frac{1}{r}} \Rightarrow \frac{v_2}{v_{\text{geo}}} \sim \sqrt{\frac{r_{\text{geo}}}{r_2}}$$

$$v_{200 \text{ km}} = v_{\text{geo}} \sqrt{\frac{r_{\text{geo}}}{r_{200 \text{ km}}}} = 3070 \sqrt{\frac{42,200 \text{ km}}{6580 \text{ km}}} = 7770 \text{ m/s}$$



5-8 Kepler's Laws ⁽¹⁶⁰⁰⁾ - Not just SUN-planet. Earth-Moon, etc.
(from Tycho Brahe's data, Kepler was nearsighted)

- ① elliptical orbit with Sun at one focus 
- ② same time, same area (conservation of angular momentum $\sum \tau = 0$ since $F_g \perp \text{motion}$)

③ T = period of planet
 a = semi-major length

$$T \sim S^{3/2}$$

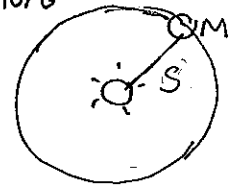
- 1650 - Newton math - see wikipedia derived the Laws from $F = ma$ polar $\frac{r}{r}$

$$\left(\frac{T_1}{T_2} \right)^2 = \left(\frac{a_1}{a_2} \right)^3$$

Derived for Uniform Circular Motion

$$\sum F = ma$$

$$G \frac{M_S M}{S^2} = \frac{M}{S} \left(\frac{2\pi S}{T} \right)^2$$



$$G \frac{M_S}{S} = \frac{4\pi^2 S}{T^2} \Rightarrow T^2 = k S^3 \Rightarrow T \sim S^{3/2}$$

ex4) $M_{\text{sun}}?$ $R_{ES} = 1.5 \times 10^{11} \text{ m}$ ③ How to measure R_{ES} ?

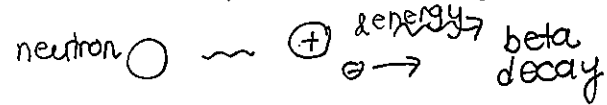
$$M_S = \frac{4\pi^2 S^3}{G T^2} = \frac{4\pi^2 (1.5 \times 10^{11})^3}{6.67 \times 10^{-11} (365.25 \times 24 \times 3600)^2} = 2.0 \times 10^{30} \text{ kg}$$

* Deviations from Kepler (perturbations) due to other planets attracting $\Rightarrow$ led to discovery by telescope of Neptune, Uranus, (Pluto)

• Moon rises an hour later each day. $T = 24\text{h}, 50\text{min}$

5-10 Four Fundamental Forces in Nature

- 1) Gravitational $\sim$ celestial
- 2) Electromagnetic $\sim$ contact force, chem
- 3) Strong nuclear force (proton / neutron)
- 4) Weak nuclear force (supernova energy given off)



- 1960s electroweak theory
- Hope for GUT grand unified electroweak & strong
TOE theory of everything - all four