

# Chapter 9 binary tree

Speaker: Lung-Sheng Chien

Reference book: Larry Nyhoff, C++ an introduction to data structures

Reference power point: Enijmax, Buffer Overflow Instruction

# OutLine

- Binary search versus tree structure
- Binary search tree and its implementation
  - insertion
  - traversal
  - delete
- Application: expression tree
  - convert RPN to binary tree
  - evaluate expression tree
- Pitfall: stack limit of recursive call

## Recall linear search in chapter 6

- Data type of **key** and **base** are immaterial, we only need to provide comparison operator. In other words, framework of linear search is independent of comparison operation.

### pseudocode

Given array  $base[0:n-1]$  and a search  $key$

$key$  and  $base$  may have different data type

for  $j = 0:1:n-1$

if  $base[j] == key$  then

return location of  $base[j]$

endfor

return not-found



User-defined comparison operation

```

#include <stdio.h>
#include <stdlib.h>
#include <string.h>
#include "key.h"
// list of all C keywords, see page 192 of textbook
keyType keytab[] = {
    {"auto"      ,0}, {"double",0}, {"int"       ,0}, {"struct"   ,0},
    {"break"    ,0}, {"else"     ,0}, {"long"     ,0}, {"switch"   ,0},
    {"case"     ,0}, {"enum"    ,0}, {"register",0}, {"typedef" ,0},
    {"char"     ,0}, {"extern",0}, {"return"   ,0}, {"union"   ,0},
    {"const"    ,0}, {"float"   ,0}, {"short"    ,0}, {"unsigned",0},
    {"continue",0}, {"for"     ,0}, {"signed"   ,0}, {"void"    ,0},
    {"default"  ,0}, {"goto"   ,0}, {"sizeof"  ,0}, {"volatile",0},
    {"do"      ,0}, {"if"     ,0}, {"static"  ,0}, {"while"   ,0}
};
// quantity NKEYS is number of keywords in array keytab
#define NKEYS ( sizeof keytab / sizeof(keyType) )

int keyword_cmp( char *keyval, keyType *datum )
{
    return strcmp( keyval, datum->word );
}

void* linear_search( const void *key, const void *base,
                    size_t n, size_t size,
                    int (*cmp)(const void *keyval, const void *atum) );

int main( int argc, char* argv[] )
{
    char key[] = "endfor" ;
    keyType *found_key ; // result of linear search

    qsort( (void*) keytab, (size_t) NKEYS, (size_t) sizeof(keyType),
           (int (*)(const void*, const void*)) &keyword_cmp );

    found_key = (keyType*) linear_search( key, keytab,
                                         NKEYS, sizeof(keyType),
                                         (int (*)(const void*, const void*)) &keyword_cmp );

    if ( NULL == found_key ){
        printf(" \"%s\" is not a keyword\n", key);
    }else{
        printf(" \"%s\" is a keyword\n", found_key->word );
    }

    return 0 ;
}

```

## linear search for structure-array

1. search **key** must be consistent with **keyval** in comparison operator, say **key** and **keyval** have the same data type, pointer to content of search key
2. **keytab[ij]** must be consistent with **\*found\_key**, they must be the same type and such type has **sizeof(keyType)** bytes

```

C:\> F:\COURSE\2008SUMMER\C_LA
"endfor" is not a keyword
Press any key to continue

```

# binary search in chapter 6

```
#include <stddef.h>

/* Given keyType array base[0], ... base[n-1]
   check if key is a keyword in array base */

void*  binsearch( const void *key, const void *base,
                 size_t n, size_t size,
                 int (*cmp)(const void *keyval, const void *datum)
                 )
{
    size_t low, high, mid ; // index of array base,
                          // always keep low < mid < high
    int cond ; // comparison result of key and base[i]
    char *a_i ; // &base[i]
    char *a = (char*) base ;

    low = 0 ; high = n ;
    while( low < high ){
        mid = low + (high - low)/2 ;
        a_i = a + size*mid ;
        cond = (*cmp)( key, a_i ) ;
        if ( 0 > cond )
            high = mid ;
        else if ( 0 < cond )
            low = mid + 1 ;
        else
            return a_i ;
    }
    return NULL ; // not found
}
```

```
#include <stddef.h>

/* Given keyType array base[0], ... base[n-1]
   check if key is a keyword in array base */

void*  linear_search( const void *key, const void *base,
                    size_t n, size_t size,
                    int (*cmp)(const void *keyval, const void *atum)
                    )
{
    size_t i ;
    char *a_i ; // &base[i]
    char *a = (char*) base ;

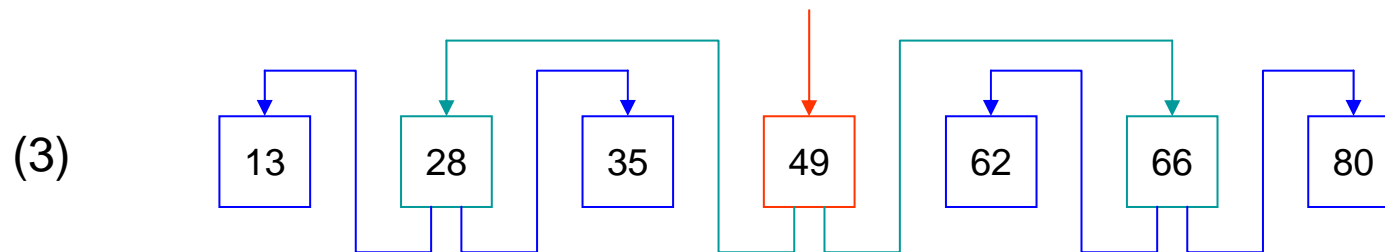
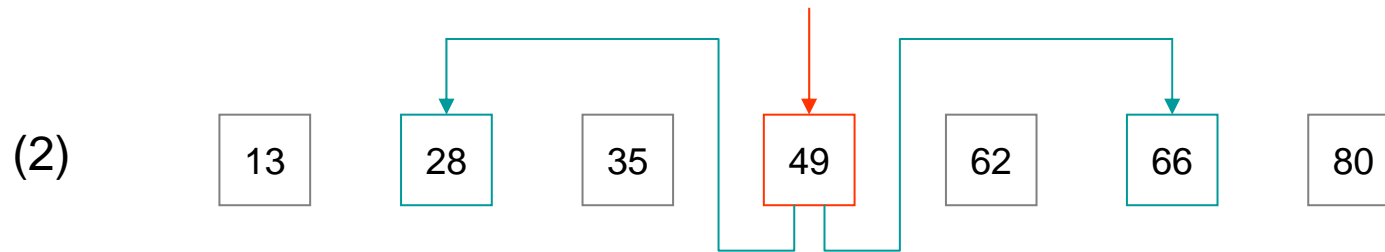
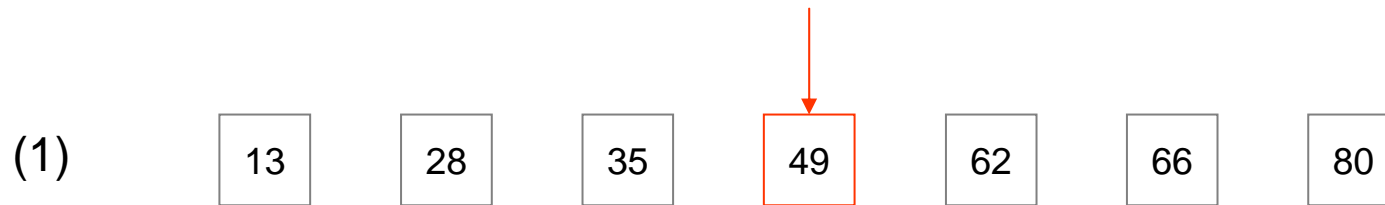
    for( i=0 ; i < n ; i++){
        a_i = a + size*i ;

        if ( 0 == (*cmp)( key, a_i ) ){
            return a_i ;
        }
    }
    return NULL ; // not found
}
```

since “**endfor**” is not a keyword, under **linear search** algorithm, we need to compare all keywords to reject “**endfor**”. We need another efficient algorithm, **binary search**, which is the best.

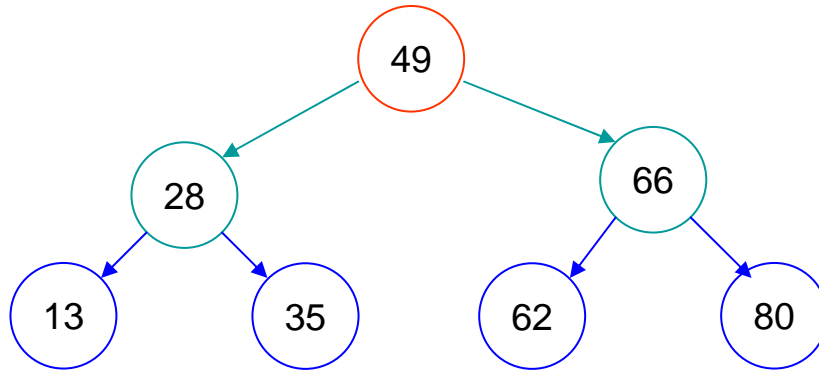
# step-by-step of binary search [1]

13	28	35	49	62	66	80
----	----	----	----	----	----	----



# step-by-step of binary search [2]

Equivalent tree structure



**Question:** Does binary-search work on sorted Linked-List?

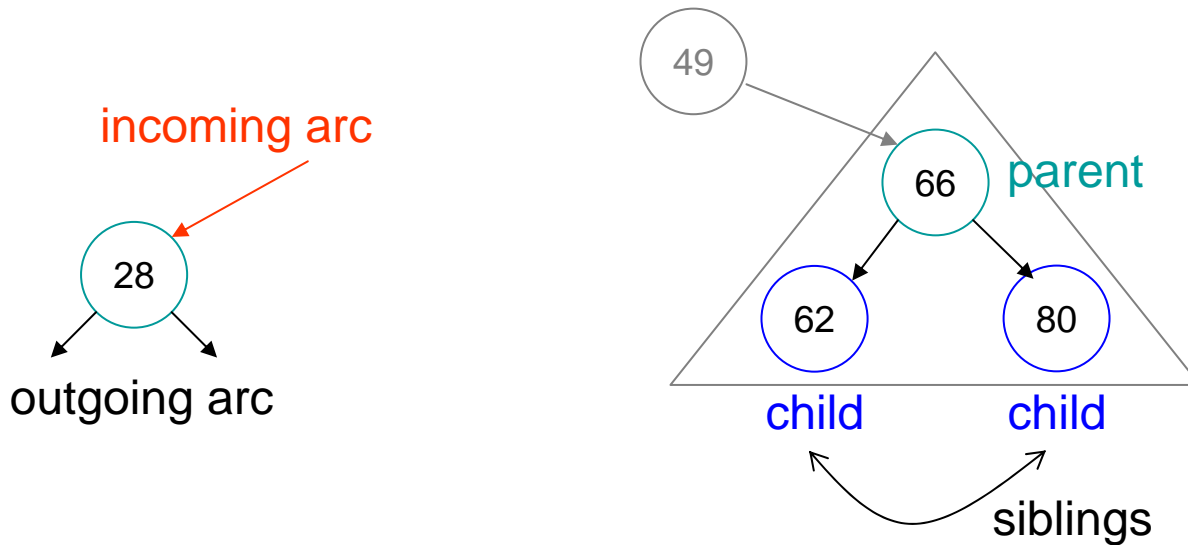
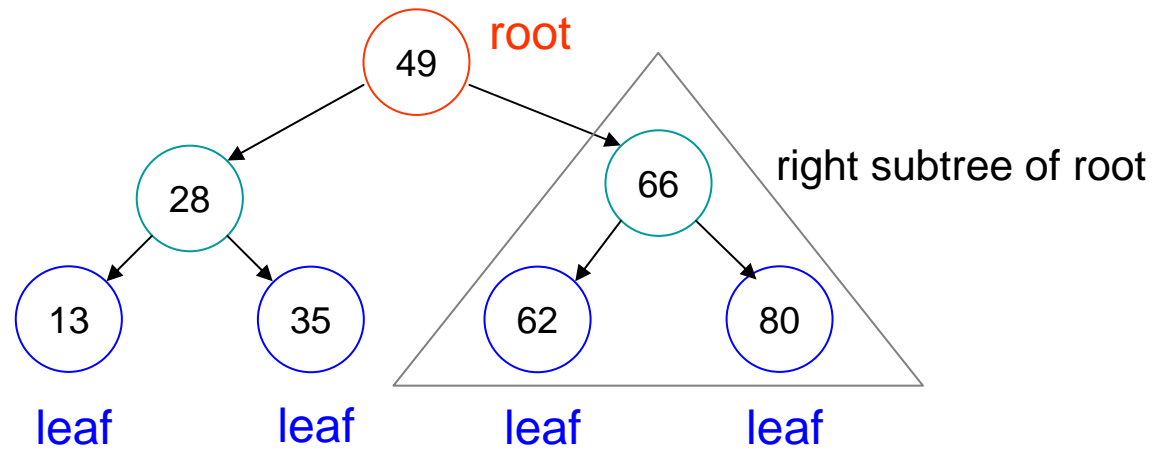


# Tree terminology [1]

- A tree consists of a finite set of elements called nodes and a finite set of directed arcs that connect pairs of nodes.
- “*root*” is one node without incoming arc, and every other node can be reached from *root* by following a unique sequence of consecutive arcs.
- Leaf node is one node without outgoing arc.
- child node is successor (繼承者) of parent node, parent node is predecessor (被繼承者) of child node
- Children with the same parent are siblings (兄弟姐妹) of each other



# Tree terminology [2]



# OutLine

- Binary search versus tree structure
- **Binary search tree and its implementation**
  - insertion
  - traversal
  - delete
- Application: expression tree
  - convert RPN to binary tree
  - evaluate expression tree
- Pitfall: stack limit of recursive call

# Binary Search Tree (BST)

- Collection of data elements (data storage)  
a binary tree in which for each node  $x$ :  
value in left child of  $x \leq$  value in  $x \leq$  value in right child of  $x$
- Basic operations (methods)
  - construct an empty BST
  - determine if BST is empty
  - *search* the BST for a given item
  - *Insert* a new item in the BST and maintain BST property
  - *delete* an item from the BST and maintain BST property
  - *Traverse* the BST and visit each node exactly once. At least one of the traversals, called an inorder traversal, must visit the values in the nodes in ascending order

# Variant of BST

- **Treap:** a [binary search tree](#) that orders the nodes by adding a random *priority* attribute to a node, as well as a key. The nodes are ordered so that the keys form a binary search tree and the priorities obey the max heap order property.
- **red-black tree:** a type of [self-balancing binary search tree](#), a [data structure](#) used in [computer science](#), typically used to implement [associative arrays](#).
- **Heap:** a specialized [tree-based data structure](#) that satisfies the *heap property*: if  $B$  is a [child node](#) of  $A$ , then  $\text{key}(A) \geq \text{key}(B)$ .
- **AVL tree:** a [self-balancing binary search tree](#).
- **B-tree:** a [tree data structure](#) that keeps data sorted and allows searches, insertions, and deletions in logarithmic [amortized](#) time. It is most commonly used in [databases](#) and [filesystems](#).
- threaded [binary tree](#) : possible to traverse the values in the [binary tree](#) via a linear traversal that is more rapid than a recursive [in-order traversal](#).

# Requirement of BST

integrate into  
structure **BST**

- **treeEle**: data type
- type of physical storage: linked-list
- ordered mechanism: depends on **treeEle**
- pointer to **root** node

Methods of  
structure **BST**

- **BST\* BST\_init( void )**
- **int empty( BST\* )**
- **int search( BST\*, treeEle )**
- **void insert( BST\*, treeEle )**
- **void remove( BST\*, treeEle )**
- **void traverse( BST\* )**

## Linked-List BST: header file

```

#ifndef BINARY_SEARCH_TREE
#define BINARY_SEARCH_TREE

typedef int treeEle ; // integer bindary tree

typedef struct BinNode {
    treeEle  data ;
    BinNode *left ;
    BinNode *right ;
}BinNode ;

typedef BinNode*  BinNodePtr ;

typedef struct {
    BinNodePtr root ;
} BST ;

// allocate a new BinNode with data = val
BinNodePtr  newBinNode( treeEle val ) ;

// construct an empty BST
BST*  BST_init( void ) ;

// return 1 if BST is empty
//      0 otherwise
int  empty( BST* ) ;

// return 1 if item is in the BST
//      0 otherwise
int  search( BST *tree, treeEle item) ;

// insert a new item in the BST and maintain BST property
void  insert( BST *tree, treeEle item ) ;

// traverse BST: inorder LNR
void  traverse_inorder( BST *tree ) ;
      void  traverse_inorder_aux( BinNodePtr node ) ;

#endif // BINARY_SEARCH_TREE

```

Type of physical storage: linked-List

pointer to root node

constructor of tree node (leaf node)

Methods of structure *BST*

# BST method: constructor (建構子)

## BST.cpp

```
#include <stdio.h>
#include <stdlib.h>
#include <assert.h>
#include "BST.h"

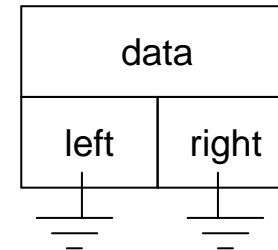
// allocate a new BinNode with data = val
BinNodePtr newBinNode( treeEle val )
{
    BinNodePtr node = (BinNodePtr) malloc(sizeof(BinNode)) ;
    assert( node ) ;

    node->data = val ;
    node->left = NULL ;
    node->right = NULL ;
}

// construct an empty BST
BST* BST_init( void )
{
    BST* tree = (BST*)malloc(sizeof(BST)) ;
    assert( tree ) ;

    tree->root = NULL ; empty tree
    return tree ;
}
```

Construct leaf node



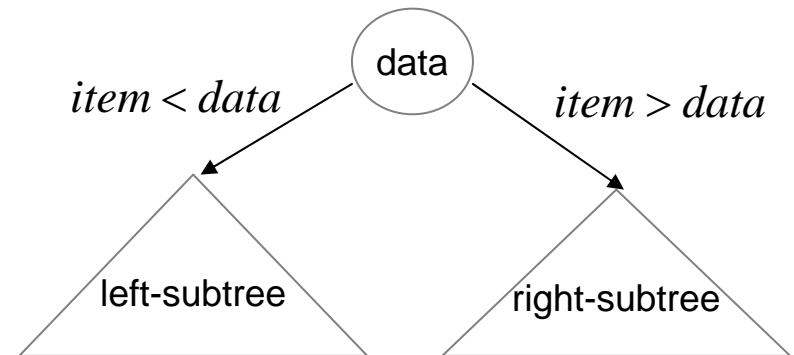
Data encapsulation: user does not **see** function *newBinNode*

# BST method: binary search

## BST.cpp

```
// return 1 if BST is empty
//      0 otherwise
int empty( BST *tree )
{
    assert( tree ) ;
    return (NULL == tree->root) ;
}

// return 1 if value is in the BST
//      0 otherwise
int search( BST *tree, treeEle item ) binary search
{
    assert( tree ) ;
    BinNodePtr locPtr = tree->root ;
    int found = 0 ;
    while(1) {
        if ( found || (NULL == locPtr) ) { break ; }
        if ( item < locPtr->data ){
            locPtr = locPtr->left ;
        }else if ( item > locPtr->data ){
            locPtr = locPtr->right ;
        }else{
            found = 1 ;
        }
    }
    return found ;
}
```

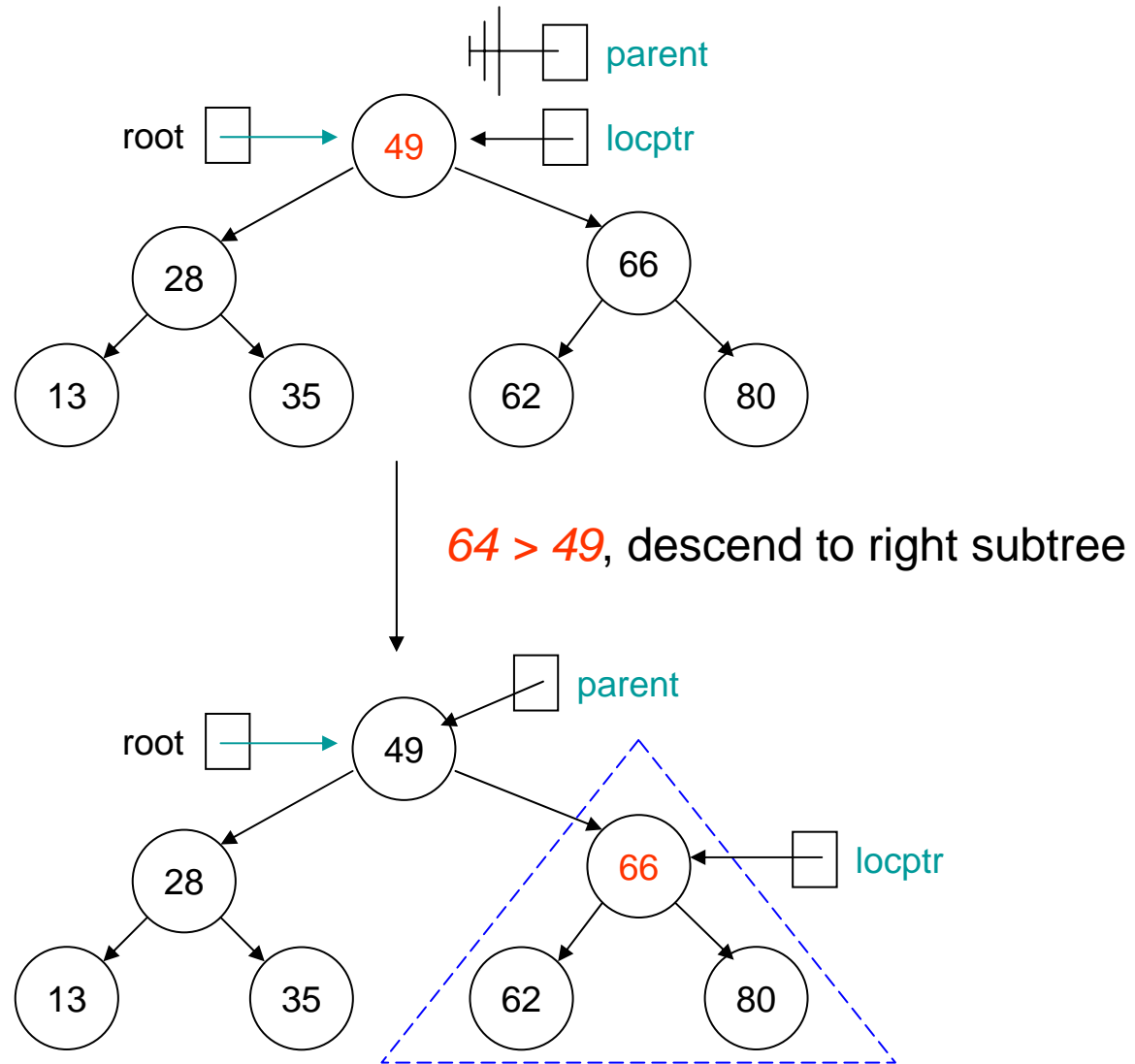




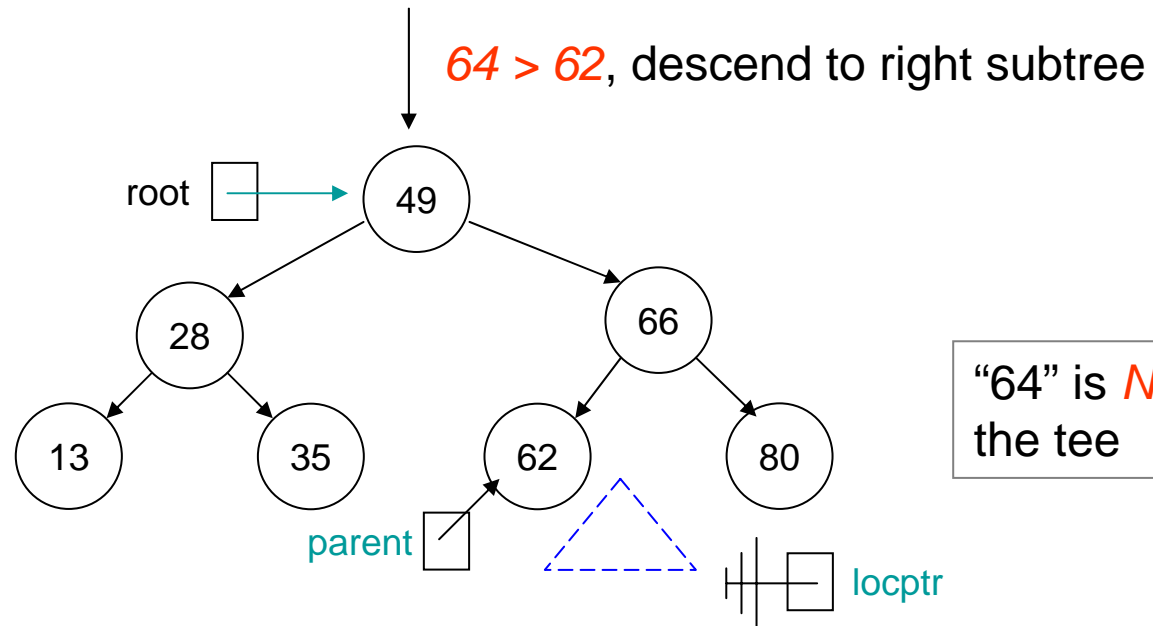
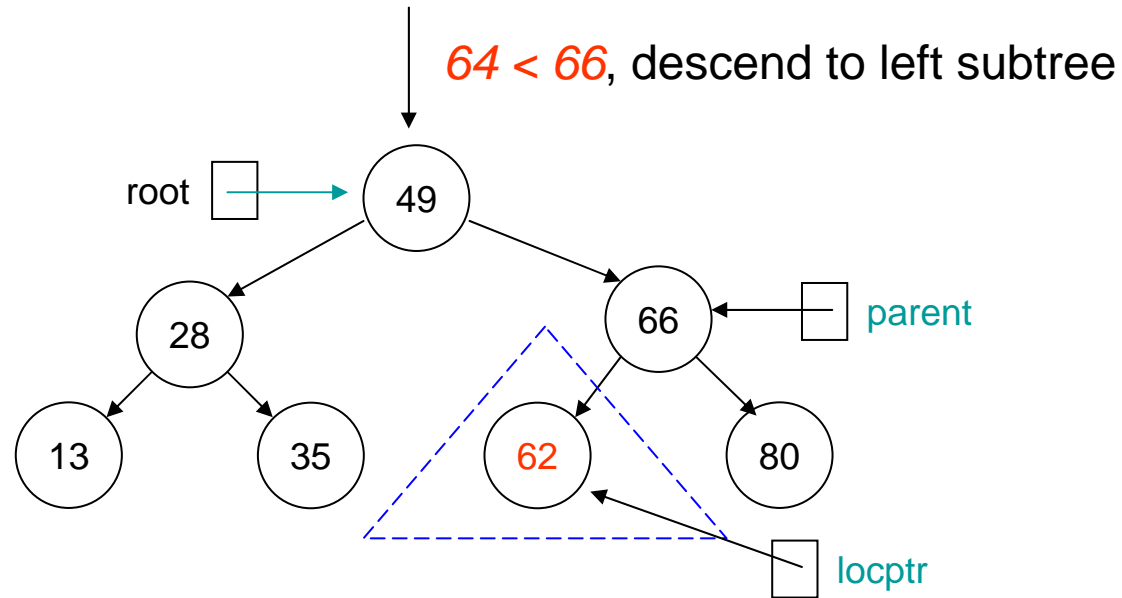
# OutLine

- Binary search versus tree structure
- Binary search tree and its implementation
  - insertion
  - traversal
  - delete
- Application: expression tree
  - convert RPN to binary tree
  - evaluate expression tree
- Pitfall: stack limit of recursive call

# BST method: insert "64" into tree [1]

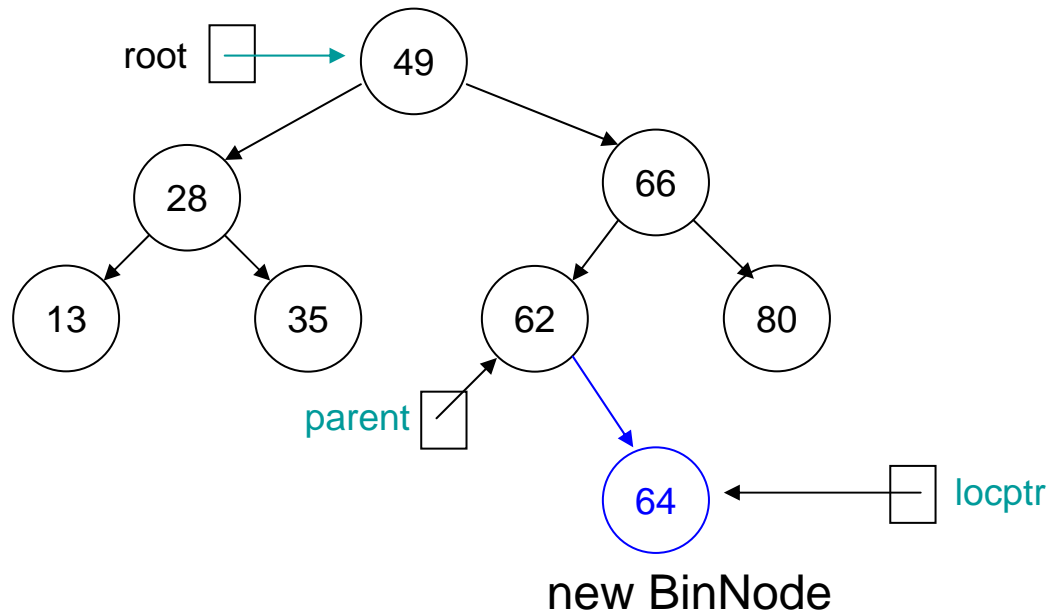


# BST method: insert "64" into tree [2]



"64" is *NOT* in the tree

## BST method: insert "64" into tree [3]



- **Step 1:** locate where a given item is to be inserted and set its parent node to pointer *parent*
- **Step 2:** construct a leaf node with data = "64" and attach to node pointed by pointer, *parent*.

# BST method: insert [4]

BST.cpp

```
// insert a new item in the BST and maintain BST property
void insert( BST *tree, treeEle item )
{
    assert( tree ) ;
    BinNodePtr locPtr = tree->root ;
    BinNodePtr parent = NULL ;
    int found = 0 ;
    while(1) {
        if ( found || (NULL == locPtr) ) { break ; }
        parent = locPtr ;
        if ( item < locPtr->data ){
            locPtr = locPtr->left ;
        }else if ( item > locPtr->data ){
            locPtr = locPtr->right ;
        }else{
            found = 1 ;
        }
    }
    if ( found ){
        printf("Item already in the tree \n");
    }else{
        locPtr = newBinNode( item ) ;
        if ( NULL == parent ){ // empty tree
            tree->root = locPtr ;
        }else if ( item < parent->data ){ // insert to left child
            parent->left = locPtr ;
        }else{ // // insert to right child
            parent->right = locPtr ;
        }
    }
}
```

step 1: locate parent node of target data

step 2: create leaf node of target data and attach to parent node

**Question:** why need we to compare item and parent->data again in step 2?

# OutLine

- Binary search versus tree structure
- Binary search tree and its implementation
  - insertion
  - traversal
  - delete
- Application: expression tree
  - convert RPN to binary tree
  - evaluate expression tree
- Pitfall: stack limit of recursive call

# Recursive definition of a binary tree

- *A binary tree is either empty or consists of a node called the root, which has pointers to two disjoint binary subtrees called the left subtree and right subtree*

## BST.cpp

```
void traverse_inorder( BST *tree )
{
    assert( tree ) ;
    traverse_inorder_aux( tree->root ) ;
    printf("\n");
}

void traverse_inorder_aux( BinNodePtr node )
{
    if ( NULL == node ) { return ; }

    traverse_inorder_aux( node->left ) ;
    printf("%d ", node->data ) ;
    traverse_inorder_aux( node->right ) ;
}
```

- *In-order traversal  
traverse the left subtree  
visit the root and process its content  
traverse the right subtree*

Termination condition

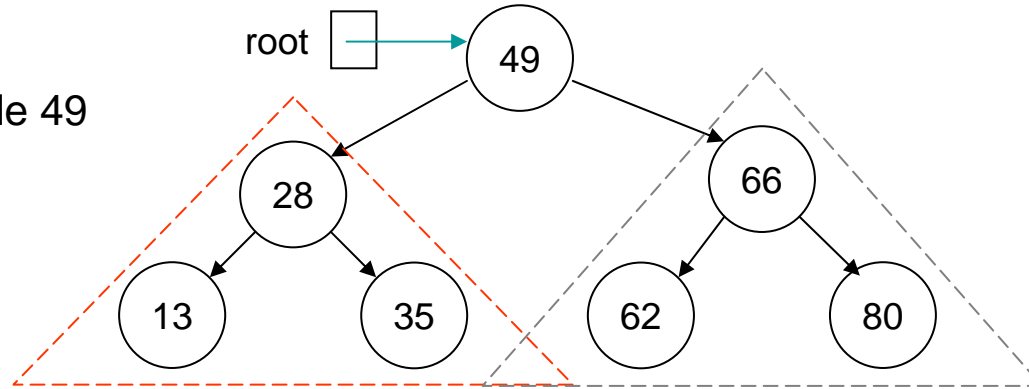
# Inorder traversal

[1]

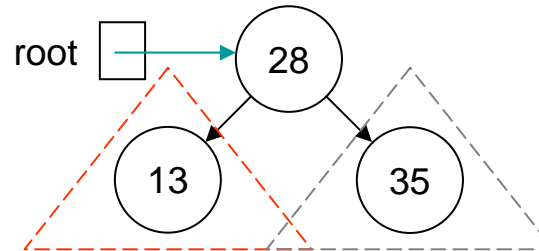
Here **root** means starting node of any tree

output

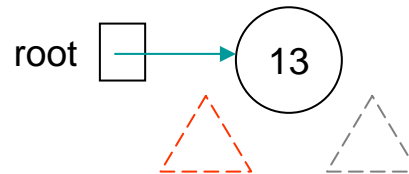
(1) goto left subtree of node 49



(2) goto left subtree of node 28



(3) goto left subtree of node 13



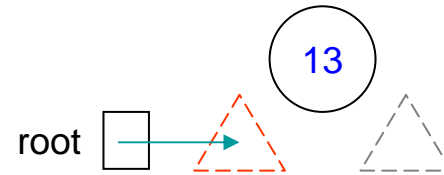


# Inorder traversal

[2]

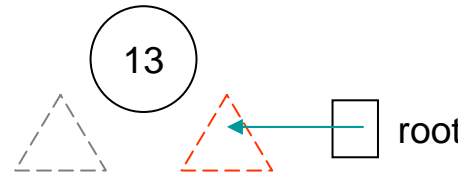
output

- (4) root is NULL, output 13  
goto right subtree of node 13



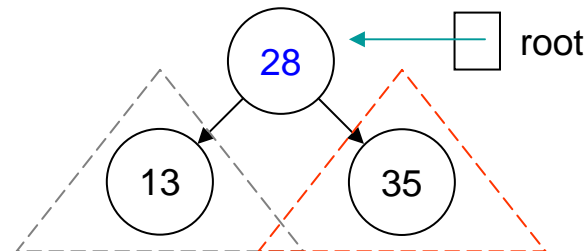
13

- (5) root is NULL, all children of node 13 have been visited, go back to node 28



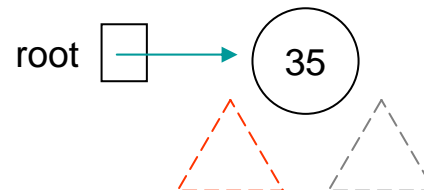
13

- (6) output node 28, goto right subtree of node 28



13,28

- (7) goto left subtree of node 35

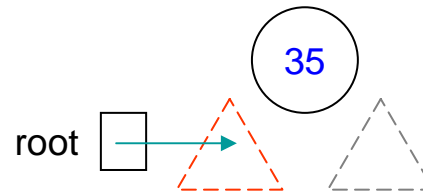


13, 28

# Inorder traversal [3]

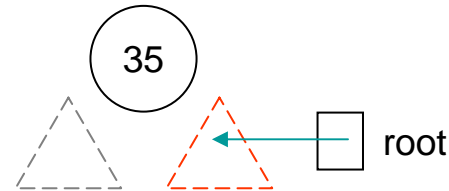
output

(8) root is NULL, output 35,  
goto right subtree of node 35



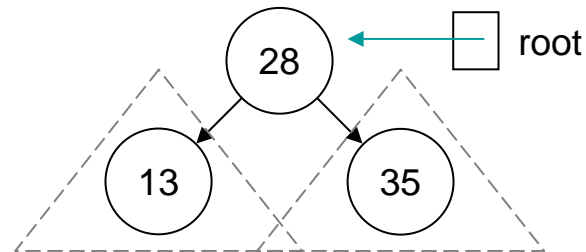
13, 28, 35

(9) root is NULL, all children of  
node 35 have been visited,  
go back to node 28



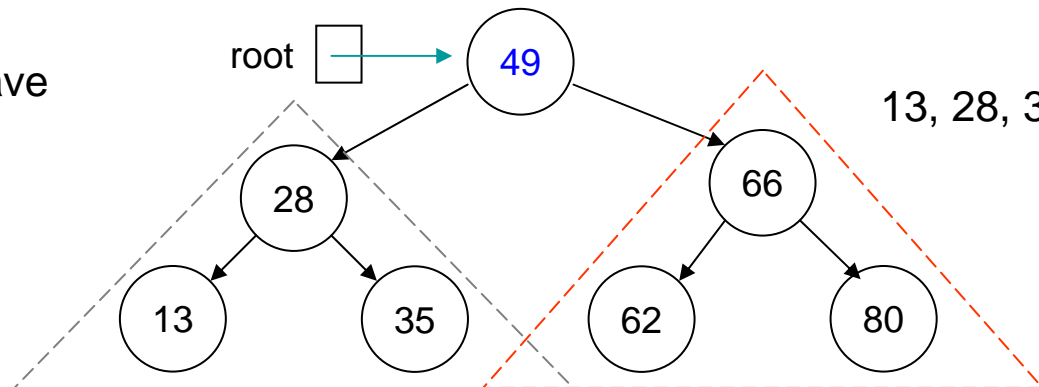
13, 28, 35

(10) All children of node 28 have  
been traversed,  
go back to node 49



13, 28, 35

(11) left-subtree of node 49 have  
been traversed, output 49  
and goto right subtree



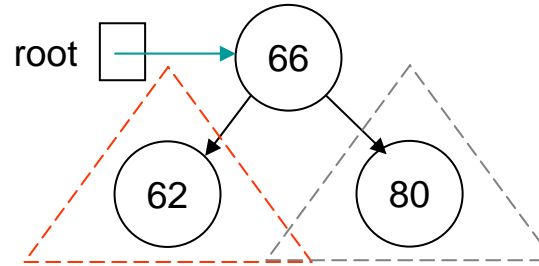
13, 28, 35, 49

# Inorder traversal

[4]

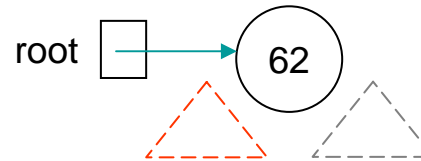
output

(12) goto left subtree of node 66



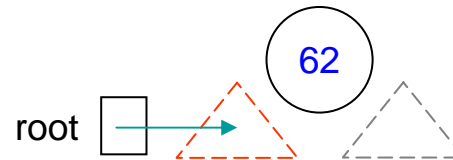
13, 28, 35, 49

(13) goto left subtree of node 62



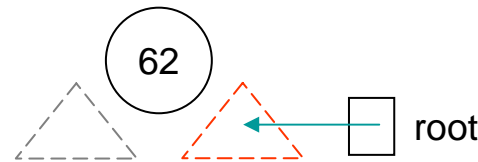
13, 28, 35, 49

(14) root is NULL, output 62,  
goto right subtree of node 62



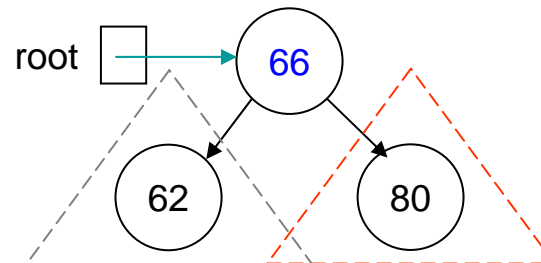
13, 28, 35, 49, 62

(15) All children of node 62 have  
been visited,  
go back to node 66



13, 28, 35, 49, 62

(16) Let subtree of node 66 is  
visited, output 66 and  
goto right subtree of node 66



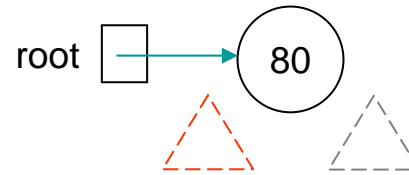
13, 28, 35, 49, 62, 66

# Inorder traversal

[5]

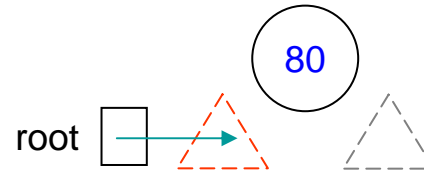
output

(17) goto left subtree of node 80



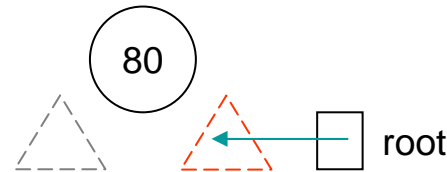
13,28,35,49,62,66

(18) root is NULL, output 80 and  
goto right subtree of node 80



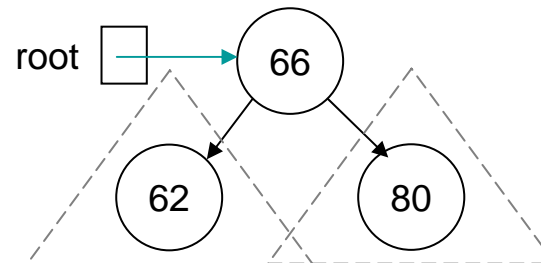
13,28,35,49,62,66,80

(19) All children of node 80 have  
been visited,  
go back to node 66



13,28,35,49,62,66,80

(20) All children of node 66 have  
been visited,  
go back to node 49



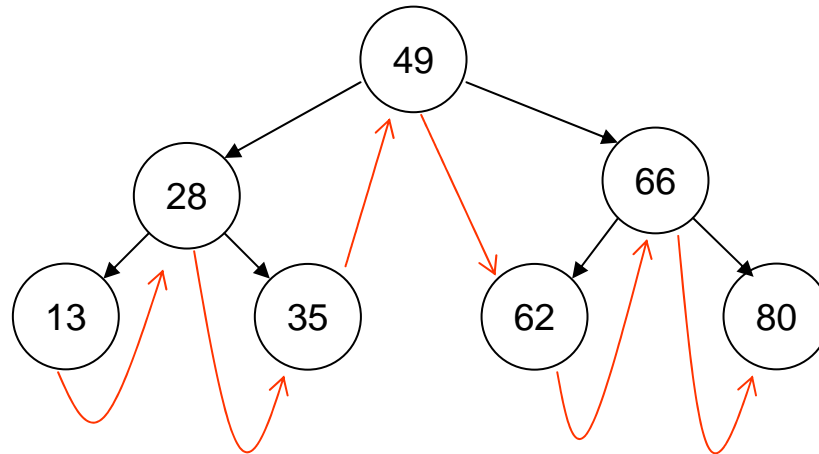
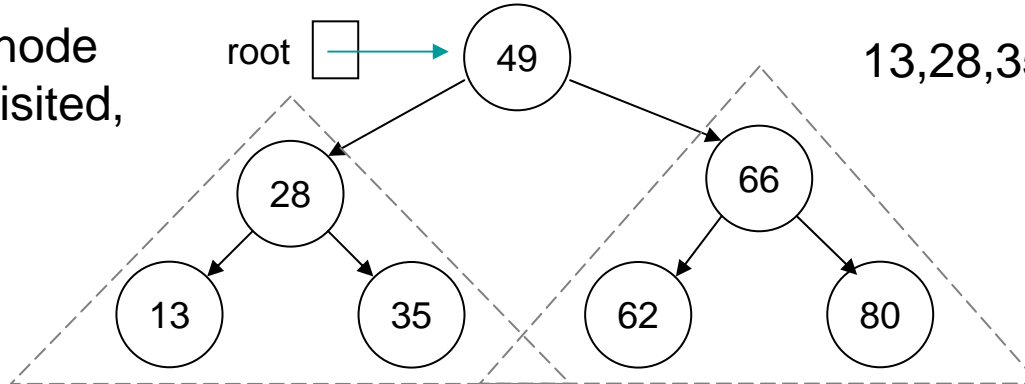
13,28,35,49,62,66,80

# Inorder traversal

[6]

output

(21) All children of node 49 have been visited, terminate



Inorder in BST is ascending order, why?

# Driver for Inorder traversal [1]

main.cpp

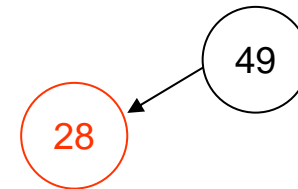
```
#include <stdio.h>
#include "BST.h"

int main( int argc, char *argv[])
{
    BST* tree = BST_init() ; 1
    if ( empty(tree) ) {
        printf("Tree is empty \n");
    }
    insert( tree, 49 ) ;
    insert( tree, 28 ) ;
    insert( tree, 13 ) ;
    insert( tree, 35 ) ;
    insert( tree, 66 ) ;
    insert( tree, 62 ) ;
    insert( tree, 80 ) ; } 2
    traverse_inorder( tree ) ; 3
    if ( search(tree, 80) ){
        printf("80 is in the tree\n");
    }
    if ( !search(tree, 12) ){
        printf("12 is NOT in the tree\n");
    }
    return 0 ;
}
```

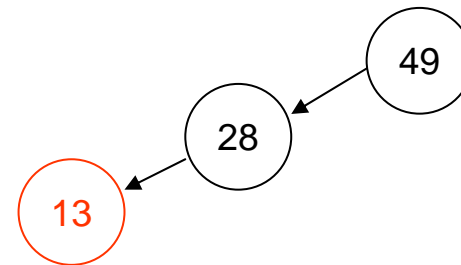
insert(tree,49)



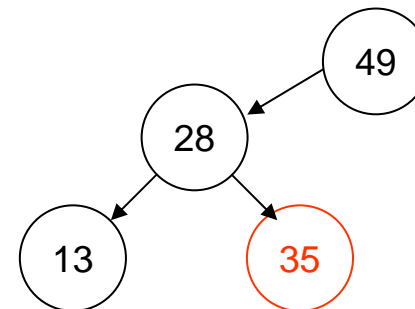
insert(tree,28)



insert(tree,13)



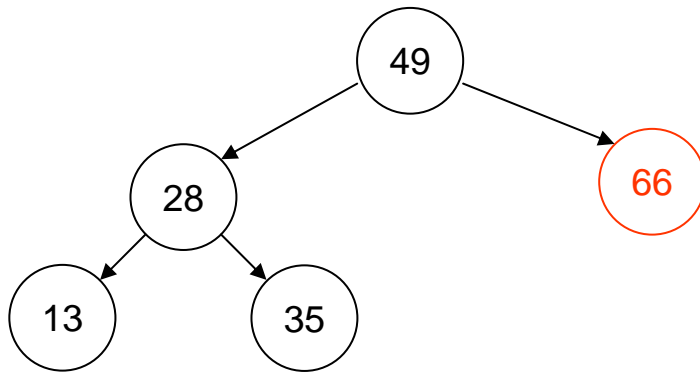
insert(tree,35)



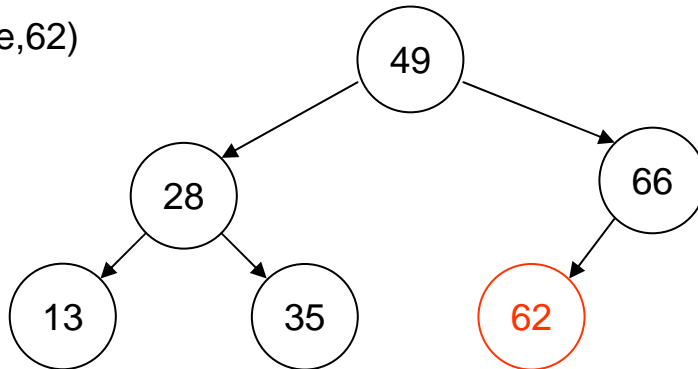
```
Tree is empty
13 28 35 49 62 66 80
80 is in the tree
12 is NOT in the tree
Press any key to continue_
```

# Driver for Inorder traversal [2]

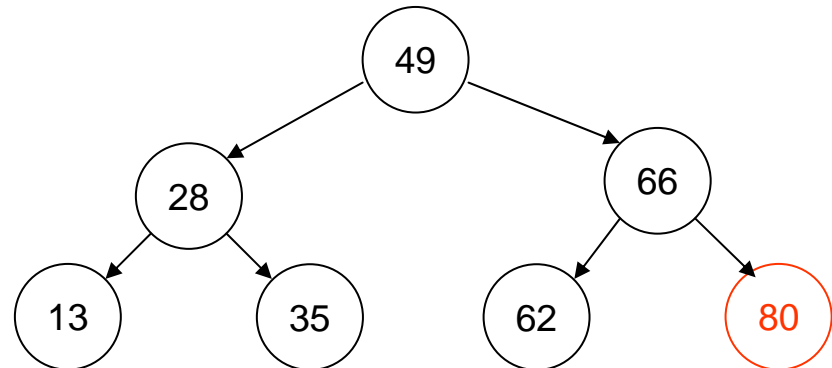
insert(tree,66)



insert(tree,62)



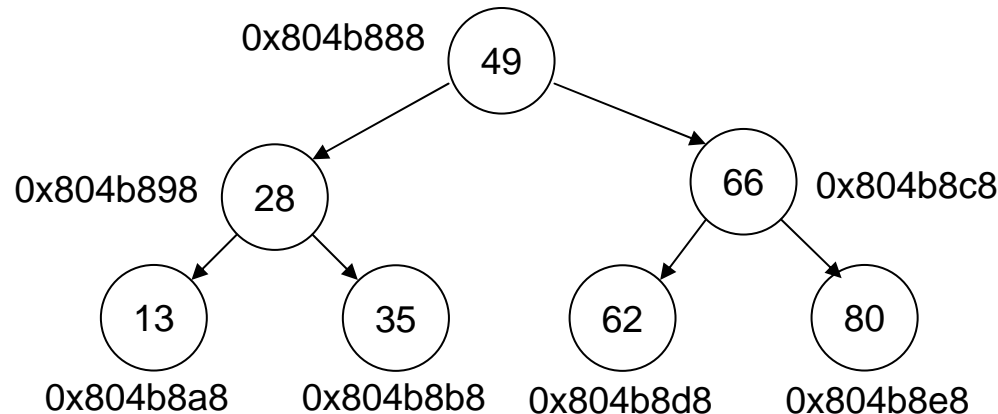
insert(tree,80)



# Exercise

- Implement integer BST with methods *newBinNode*, *BST\_init*, *empty*, *search*, *insert* as we discuss above and write a method (function) to show configuration of BST as follows.

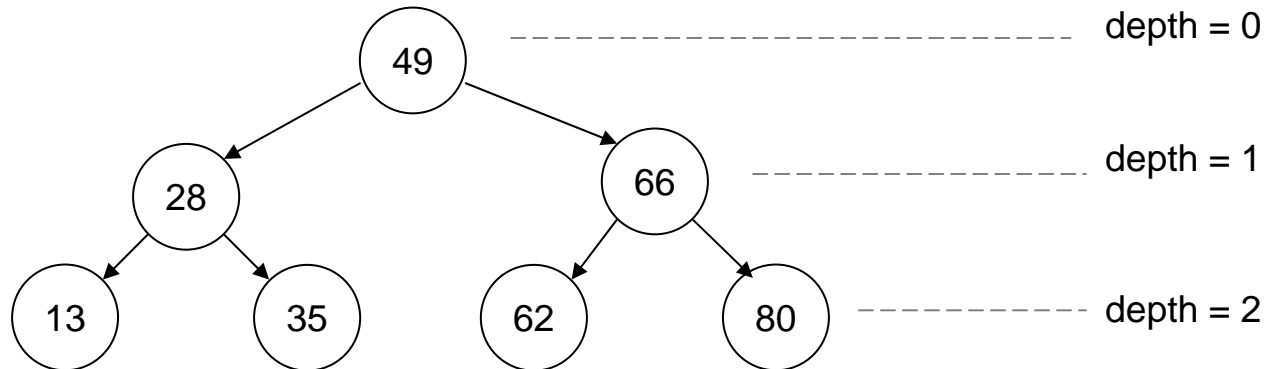
address	data	left node	right node
0x804b888	49	0x804b898	0x804b8c8
0x804b898	28	0x804b8a8	0x804b8b8
0x804b8a8	13	(nil)	(nil)
0x804b8b8	35	(nil)	(nil)
0x804b8c8	66	0x804b8d8	0x804b8e8
0x804b8d8	62	(nil)	(nil)
0x804b8e8	80	(nil)	(nil)





# Exercise

- Use recursive call to implement methods *search* and *insert*.
- Write a method to compute maximum depth of a BST.



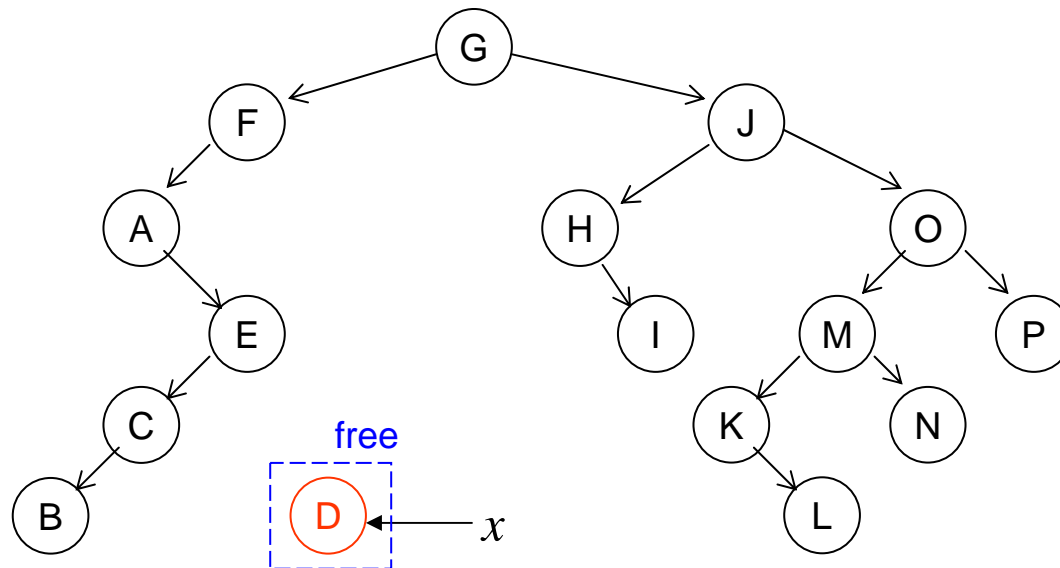
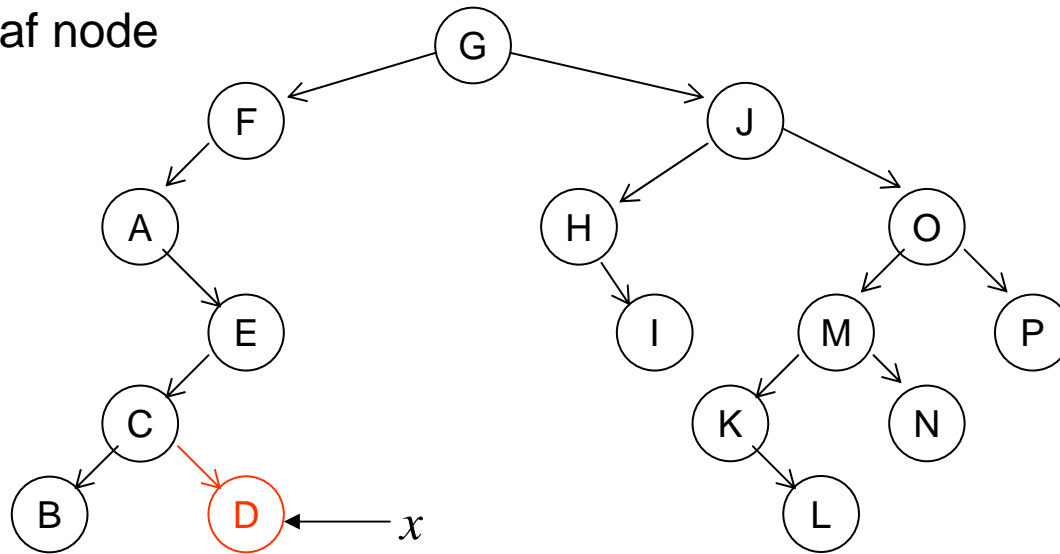
- What is topology of a BST created by inserting 13, 28, 35, 49, 62, 66, 80 in turn.
- Can you modify an unbalanced BST into a balanced one?

# OutLine

- Binary search versus tree structure
- Binary search tree and its implementation
  - insertion
  - traversal
  - delete
- Application: expression tree
  - convert RPN to binary tree
  - evaluate expression tree
- Pitfall: stack limit of recursive call

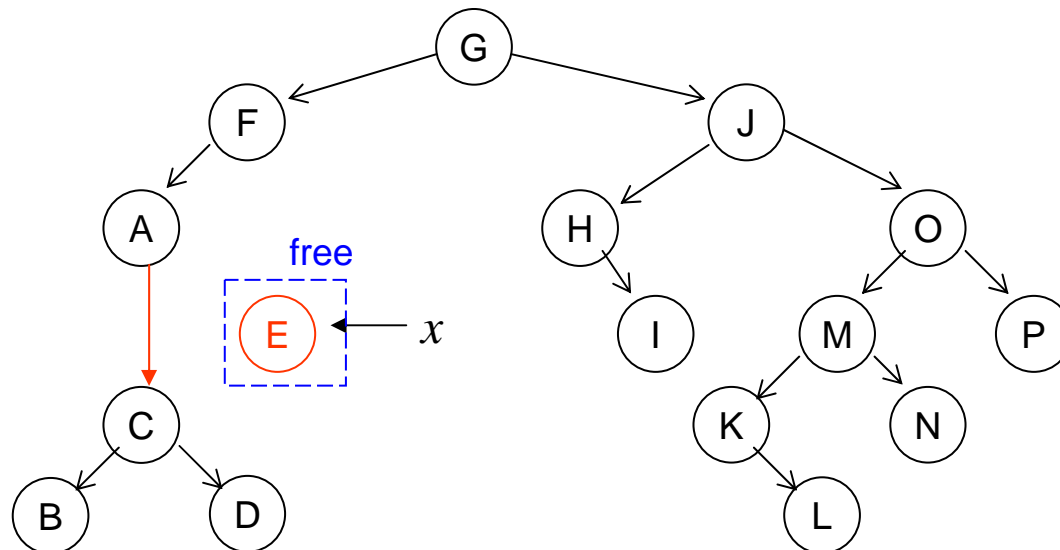
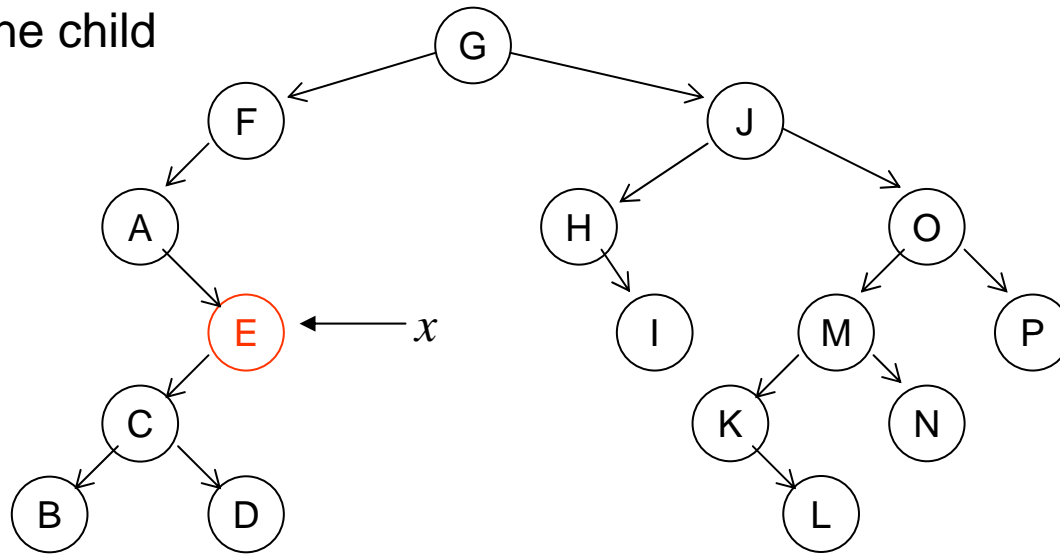
# Delete a node x from BST [1]

case 1: x is a leaf node



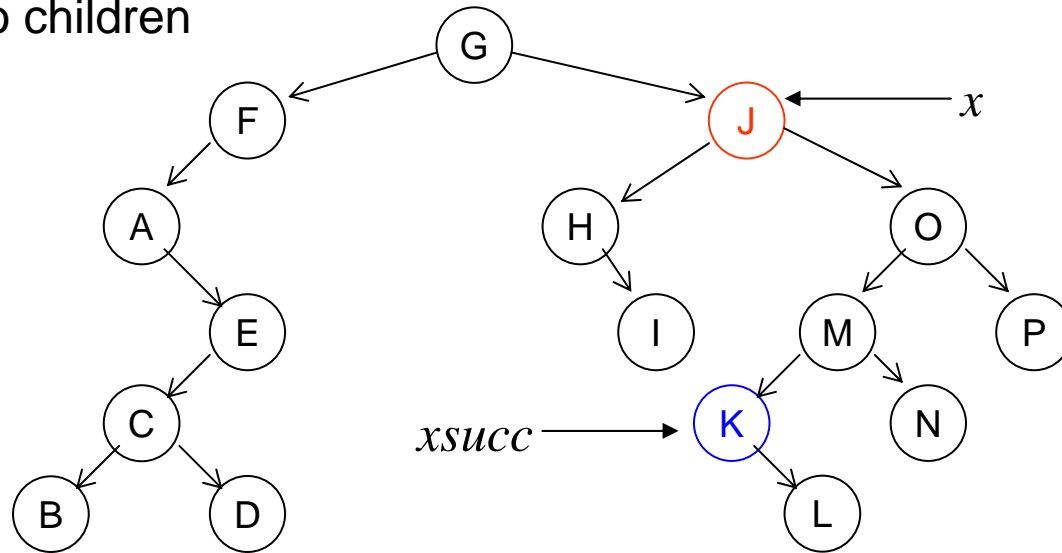
# Delete a node x from BST [2]

case 2: x has one child

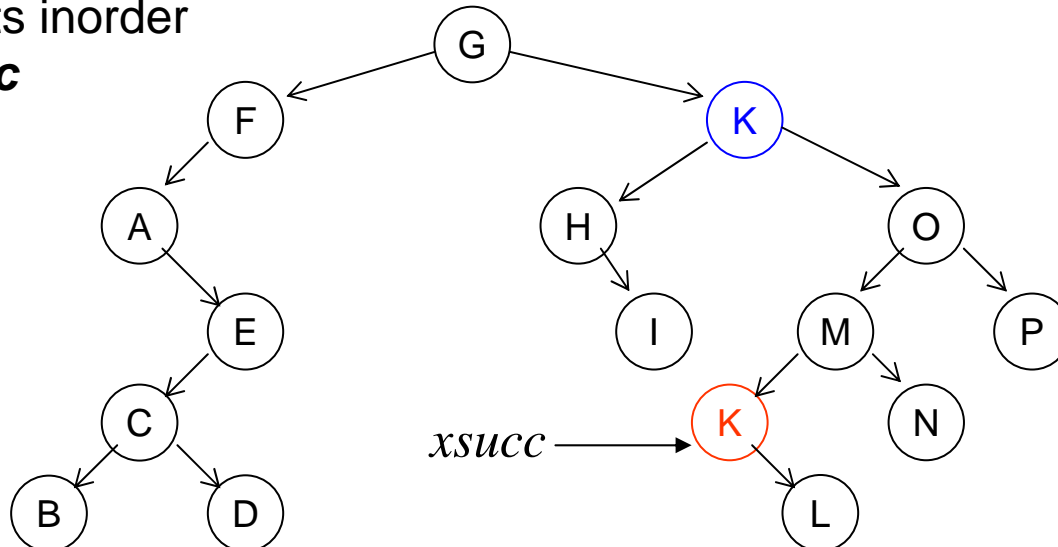


# Delete a node x from BST [3]

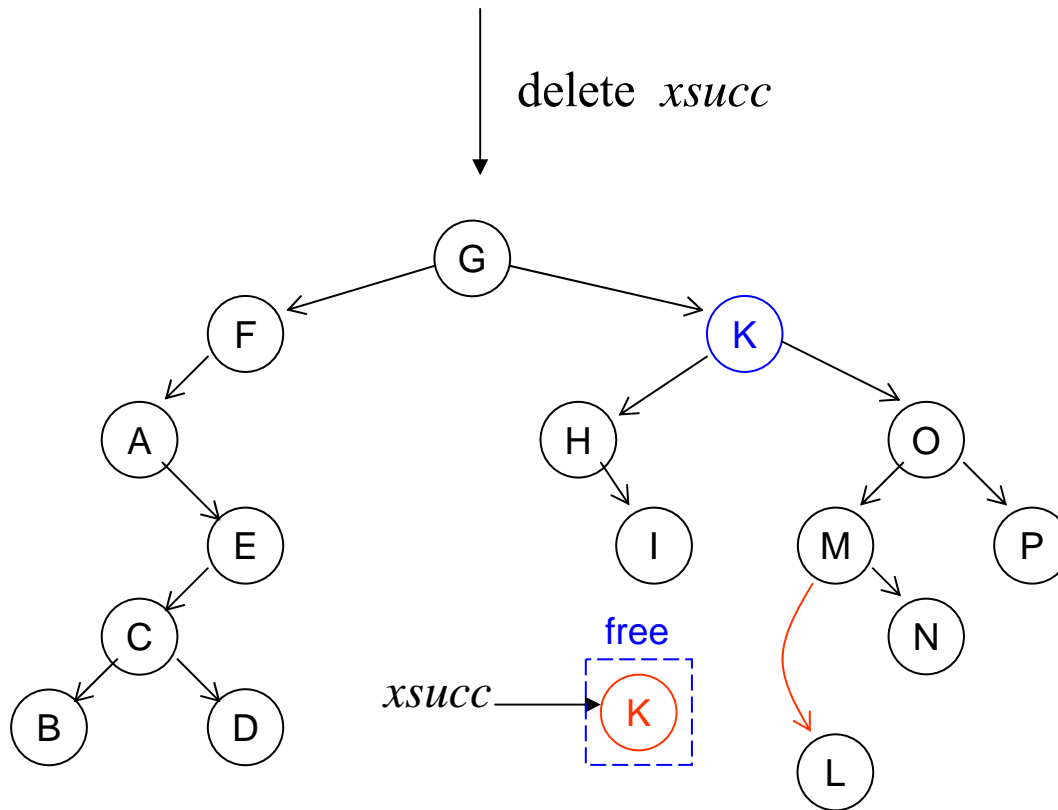
case 3: x has two children



Replace x with its inorder successor ***xsucc***



# Delete a node x from BST [4]



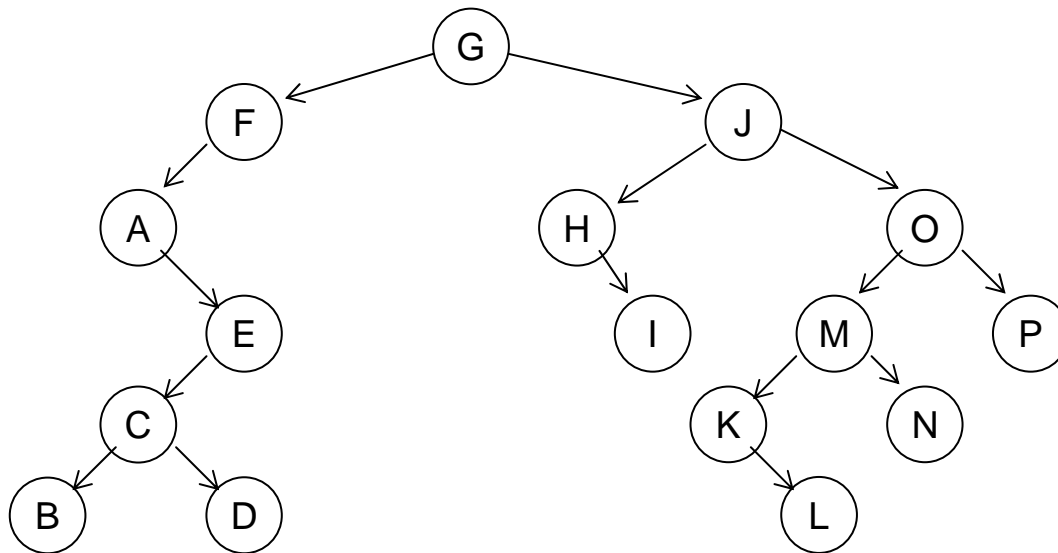
## BST method: remove item

```
void remove( BST *tree, treeEle item )
{
    int found ;
    BinNodePtr x, parent ;
    found = search2( tree, item, &x, &parent ) ;
    if ( !found ){
        printf("Item is not in the BST \n");
        return ;
    }
    if ( (NULL != x->left) && (NULL != x->right) ){
// x has two children
// find x's inorder successor and its parent
        BinNodePtr xsucc = x->right ;
        parent = x ;
        while( NULL != xsucc->left ){
            parent = xsucc ;
            xsucc = xsucc->left ;
        }
// move content of xsucc to x and change x to
// point to successor which will be deleted
        x->data = xsucc->data ;
        x = xsucc ;
    } // if x has two children
// proceed with case where node x has 0/1 child
    BinNodePtr subtree = x->left ;
    if ( NULL == subtree){
        subtree = x->right ;
    }
    if ( NULL == parent ){
        tree->root = subtree ;
    } else if ( x == parent->left ){
        parent->left = subtree ;
    } else{
        parent->right = subtree ;
    }
    free(x) ;
}
```

```
// locates node containing an item and its parent
int search2( BST *tree, treeEle item,
            BinNodePtr *locPtr, BinNodePtr *parent )
{
    assert( tree ) ;
    *locPtr = tree->root ;
    *parent = NULL ;
    int found = 0 ;
    while(1) {
        if ( found || (NULL == locPtr) ) { break ; }
        if ( item < (*locPtr)->data ){
            *parent = *locPtr ;
            *locPtr = (*locPtr)->left ;
        } else if ( item > (*locPtr)->data ){
            *parent = *locPtr ;
            *locPtr = (*locPtr)->right ;
        } else{
            found = 1 ;
        }
    }
    return found ;
}
```

# Exercise

- Implement method *remove* and write a driver to test it, you can use following BST as test example.  
Note: you need to test all boundary cases
- Use recursive call to implement methods *remove*.

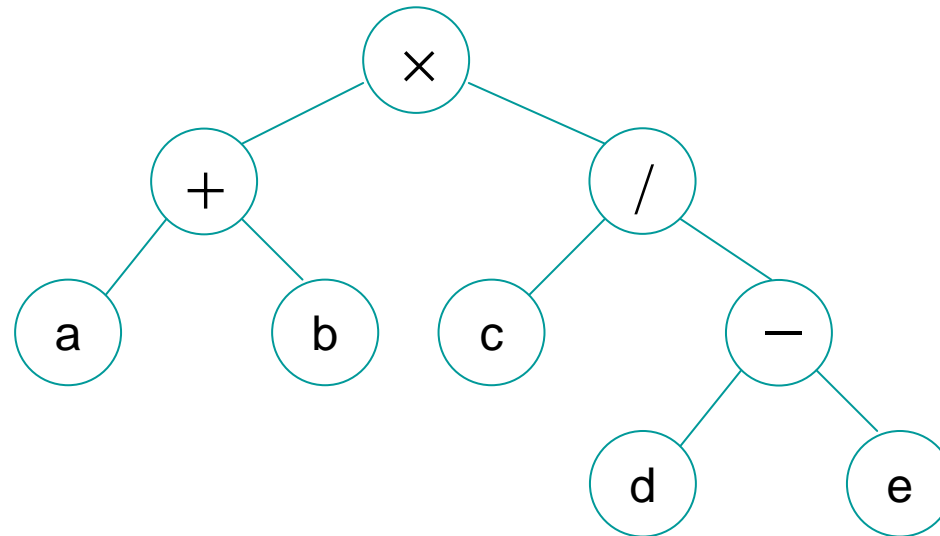




# Exercise

- Construct following expression tree (note that you may need general binary tree, not BST) and show its configuration.
- Show result of pre-order (prefix), in-order (infix) and post-order (postfix) respectively.



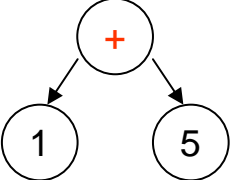
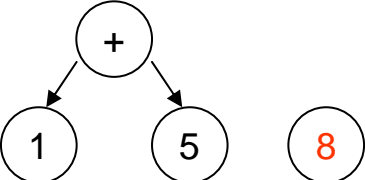
$$(a + b) \times (c / (d - e))$$



# OutLine

- Binary search versus tree structure
- Binary search tree and its implementation
  - insertion
  - traversal
  - delete
- Application: expression tree
  - convert RPN to binary tree
  - evaluate expression tree
- Pitfall: stack limit of recursive call

# Convert RPN expression to expression tree [1]

expression	stack	comments	Binary tree
15+841--×	1 ← top	Create leaf node 1 and push address onto stack	
5+841--×	5 1 ← top	Create leaf node 5 and push address onto stack	
+841--×	← top	Create node "+" and pop 5, 1 from stack as its children.	
	+ ← top	Push address of node "+" to stack	
841--×	8 + ← top	Create leaf node 8 and push address onto stack	

# Convert RPN expression to expression tree [2]

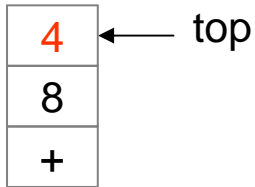
expression

stack

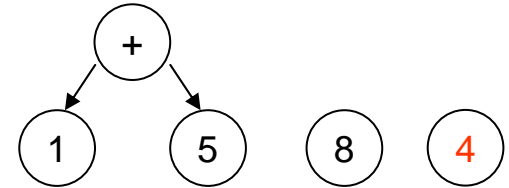
comments

Binary tree

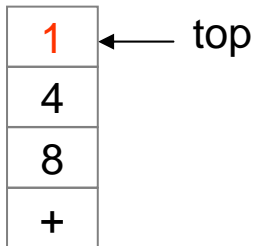
41--x



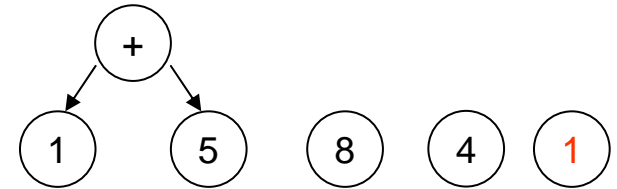
Create leaf node 4 and push address onto stack



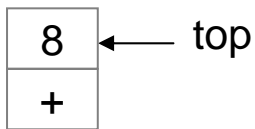
1--x



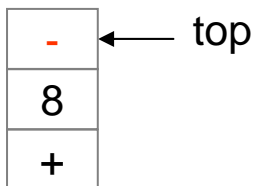
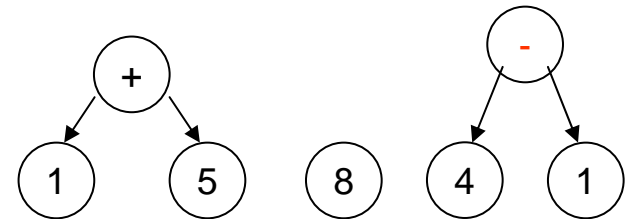
Create leaf node 1 and push address onto stack



--x



Create node "-" and pop 1, 4 from stack as its children.



Push node '-' onto stack

# Convert RPN expression to expression tree [3]

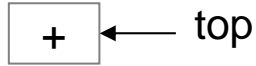
expression

stack

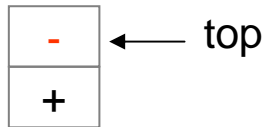
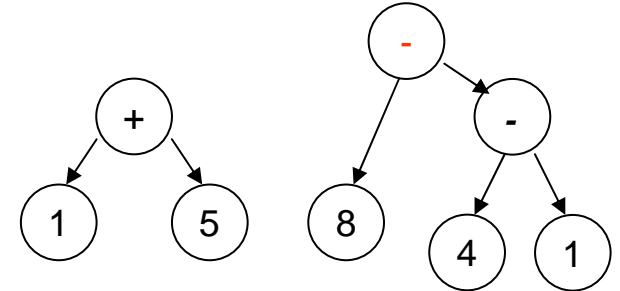
comments

Binary tree

-x

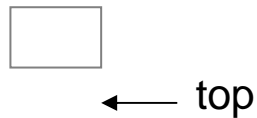


Create node "-" and pop "-", 8 from stack as its children.

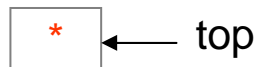
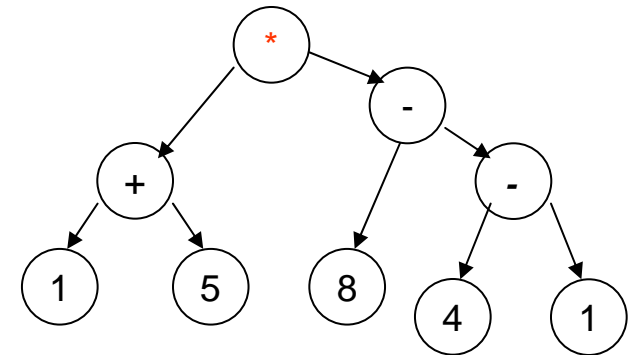


Push node "-" onto stack

x



Create node "\*" and pop "-", "+" from stack as its children.



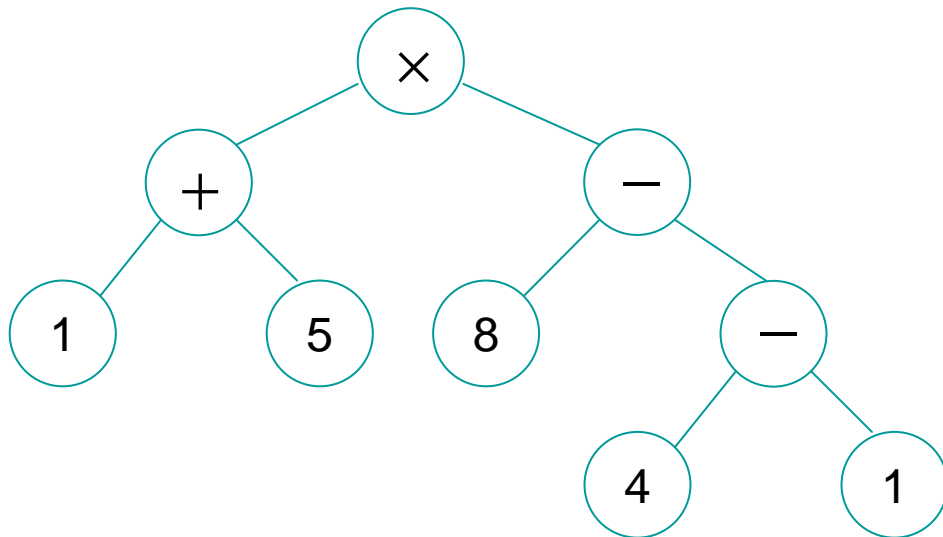
Push node "\*" onto stack



Only one address on the stack, this address is **root** of the tree

# Exercise

- Depict flow chart of “convert RPN expression to expression tree”.
- Write program to do “convert RPN expression to expression tree”, you can use following expression tree as test example.
- Use above binary tree to evaluate result (stack free, just traverse the binary tree).



infix:  $(1 + 5) \times (8 - (4 - 1))$

postfix:  $15 + 841 - - \times$

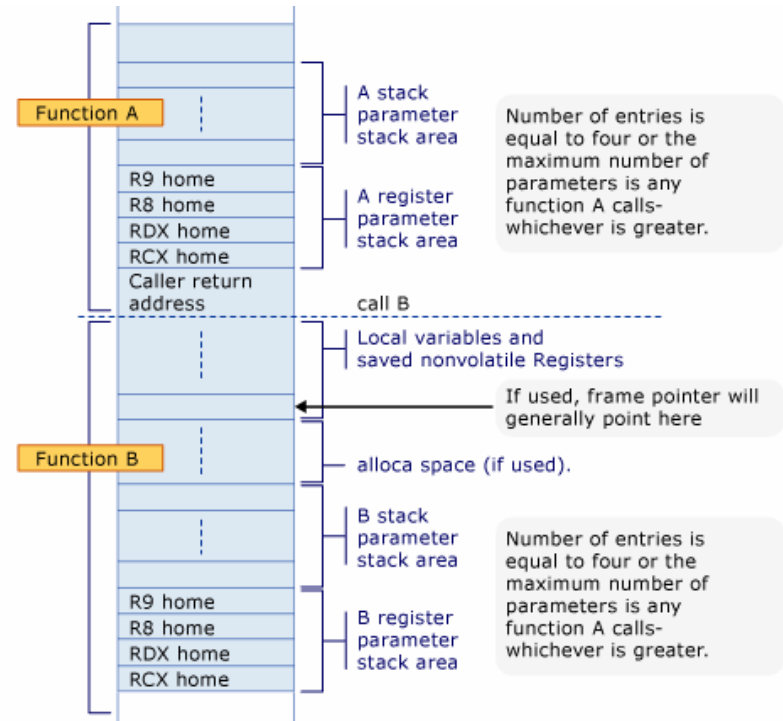
parenthesis free

# OutLine

- Binary search versus tree structure
- Binary search tree and its implementation
  - insertion
  - traversal
  - delete
- Application: expression tree
  - convert RPN to binary tree
  - evaluate expression tree
- Pitfall: stack limit of recursive call

# Stack allocation in VC2005

- A function's prolog (prolog code sequence 起始設定) is responsible for allocating stack space for local variables, saved registers, stack parameters, and register parameters.
- The parameter area is always at the bottom of the stack, so that it will always be adjacent to the return address during any function call.
- The stack will always be maintained 16-byte aligned, except within the prolog (for example, after the return address is pushed), and except where indicated in [Function Types](#) for a certain class of frame functions.
- When you define a local variable, enough space is allocated on the stack frame to hold the entire variable, this is done by compiler.
- Frame variables are automatically deleted when they go out of scope. Sometimes, we call them **automatic variables**.





# Stack frame by g++

g++ -O0 main.cpp

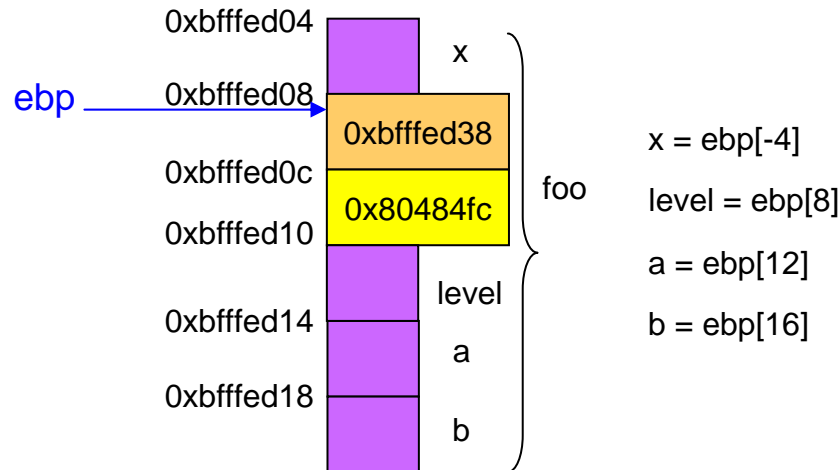
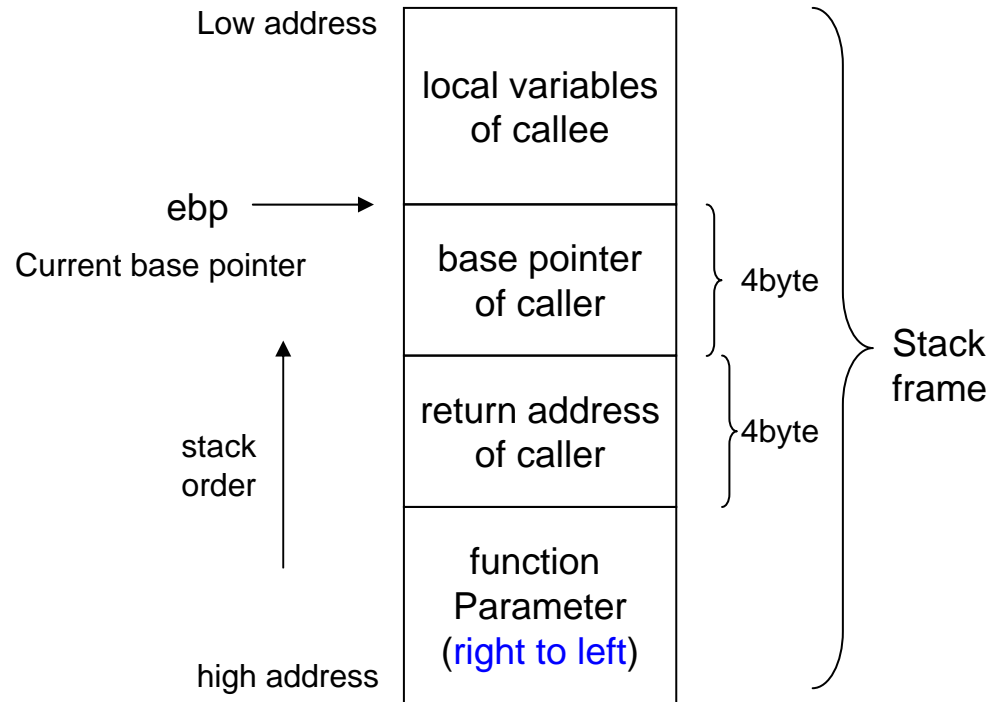
```
int foo( int level, int a, int b ) ;

int main( int argc, char* argv[] )
{
    int level = 3 ;
    int a = 2 ;
    int b = 3 ;
    foo( level, a, b ) ;
    return 0 ;
}

int foo( int level, int a, int b )
{
    int x ;
    x = a + b ;
    if ( 0 >= level ) { return x ; }
    return b * foo( level - 1, a-1, b-1 ) ;
}
```

caller: 呼叫者, 如 main

callee: 被呼叫者, 如 foo



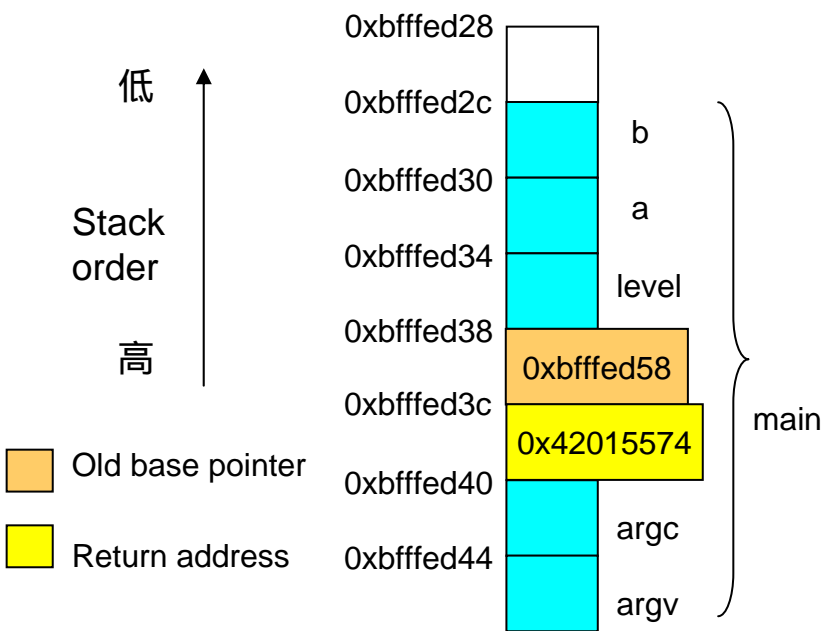
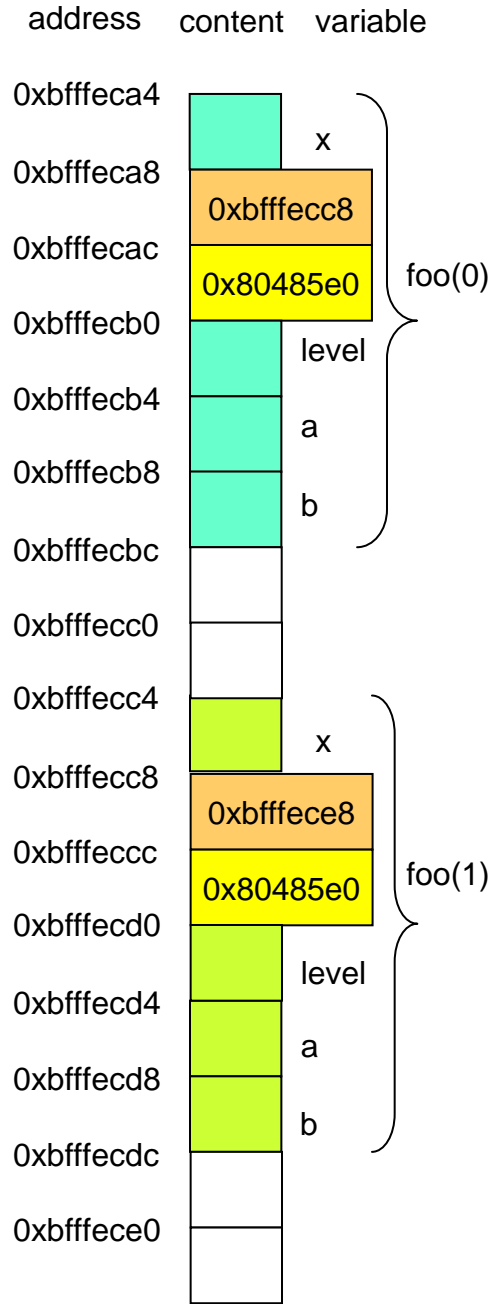
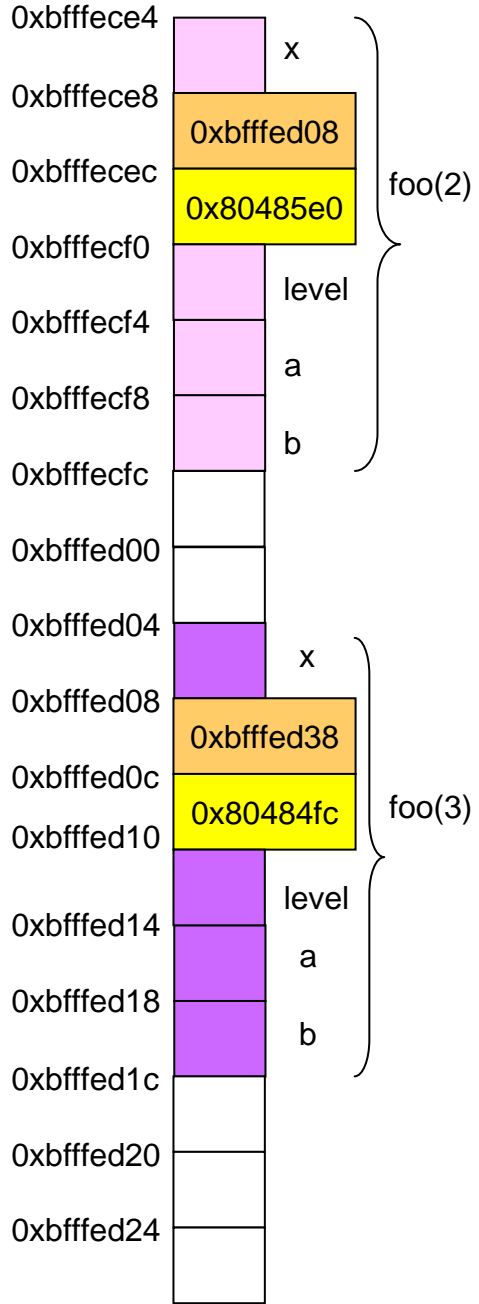
```

int foo( int level, int a, int b ) ;

int main( int argc, char* argv[] )
{
    int level = 3 ;
    int a = 2 ;
    int b = 3 ;
    foo( level, a, b ) ;
    return 0 ;
}

int foo( int level, int a, int b )
{
    int x ;
    x = a + b ;
    if ( 0 >= level ) { return x ; }
    return b * foo( level - 1, a-1, b-1 ) ;
}

```



Stack order  
 低 ↑  
 高

# Actions to call a function

- Caller push parameters of callee to stack
- Caller execute command *call*, for example “call `_Z3fooi`”.
  - push return address (address of caller) to stack
  - program counter points to function code address
- In callee
  - push old *ebp* (base pointer of caller) to stack
  - copy *esp* to *ebp* (ex: `movl %esp, %ebp`)
  - reserve enough space for local variables
- When function return to caller
  - callee move *sp* (*stack pointer*) to return address
  - callee execute command *ret*, and then program counter points to return address
  - caller pop base pointer to restore original status

# Cost to call a function

- Function calls (including parameter passing and placing object's address on the stack)
- Preservation of caller's stack frame
- Return-value communication
- Old stack-frame restore
- Return (give program control back to caller)
  
- recursive call is easy to implement and code size is minimum, however we need to pay a little overhead. That's why we do not like recursive call when dealing with computational intensive task.

**Exercise:** write quick sort with recursive version and non-recursive version, then compare performance between them.

# Exercise

- Modify following code to show address of function parameter, local variable and content of return address, base pointer.  
Use “g++ -O0” to compile your code on workstation and check configuration of stack frame.
- What is configuration of stack frame using icpc –O0 ?
- What is configuration of stack frame in VC6.0 ?
- Is configuration of stack frame the same for each execution? Why?
- What’s size of function prolog for compiler g++, icpc and vc6?

```
int foo( int level, int a, int b ) ;

int main( int argc, char* argv[] )
{
    int level = 3 ;
    int a = 2 ;
    int b = 3 ;
    foo( level, a, b ) ;
    return 0 ;
}

int foo( int level, int a, int b )
{
    int x ;
    x = a + b ;
    if ( 0 >= level ) { return x ; }
    return b * foo( level - 1, a-1, b-1 ) ;
}
```

# Stack limit

- In RedHat 9, 32-bit machine, default stack size is 8MB. Use command “ulimit -a” to show this information.
- Visual studio C++ 6.0, default stack size is 1MB

## /F (Set Stack Size)

[Home](#) | [Overview](#) | [How Do I](#) | [Compiler Options](#)

The `/Fnumber` option sets the program stack size to a specified number of bytes. If you don't specify this option, a stack size of 1 MB is used by default. The `number` argument can be in decimal or C-language notation. The argument can range from a lower limit of one to the maximum stack size accepted by your linker. (The linker rounds up the specified value to the nearest 4 bytes.) A space is optional between `/F` and `number`.

You can also set stack size by using the linker's `/STACK` option or by running `EDITBIN` on an `.EXE` file.

You may want to increase the stack size if your program gets stack-overflow diagnostic messages.

```
[ims1@linux tree_int]$ ulimit -a
core file size          (blocks, -c) 0
data seg size           (kbytes, -d) unlimited
file size               (blocks, -f) unlimited
max locked memory      (kbytes, -l) unlimited
max memory size        (kbytes, -m) unlimited
open files              (-n) 1024
pipe size               (512 bytes, -p) 8
stack size              (kbytes, -s) 8192
cpu time                (seconds, -t) unlimited
max user processes     (-u) 7168
virtual memory          (kbytes, -v) unlimited
[ims1@linux tree_int]$
```

# Test stack limit in VC6.0

```
#include <stdio.h>

#define MAXBUFFER 1024

void foo( int level ) ;

int main(int argc, char* argv[])
{
    foo(1024) ;
    return 0 ;
}

void foo( int level )
{
    char word[MAXBUFFER] ; // 1kB buffer in stack frame

    if ( 0 >= level ) { return ; }
    printf("word[last] = %c, level = %d\n",
        word[MAXBUFFER-1], level);
    foo( level-1 ) ;
}
```

Recursive call

```
word[last] = ? level = 118
word[last] = ? level = 117
word[last] = ? level = 116
word[last] = ? level = 115
word[last] = ? level = 114
word[last] = ? level = 113
word[last] = ? level = 112
word[last] = ? level = 111
word[last] = ? level = 110
word[last] = ? level = 109
word[last] = ? level = 108
word[last] = ? level = 107
word[last] = ? level = 106
word[last] = ? level = 105
word[last] = ? level = 104
word[last] = ? level = 103
word[last] = ? level = 102
word[last] = ? level = 101
word[last] = ? level = 100
word[last] = ? level = 99
word[last] = ? level = 98
word[last] = ? level = 97
word[last] = ? level = 96
word[last] = ? level = 95
Press any key to continue
```

Level number cannot reach 1  
since stack overflow

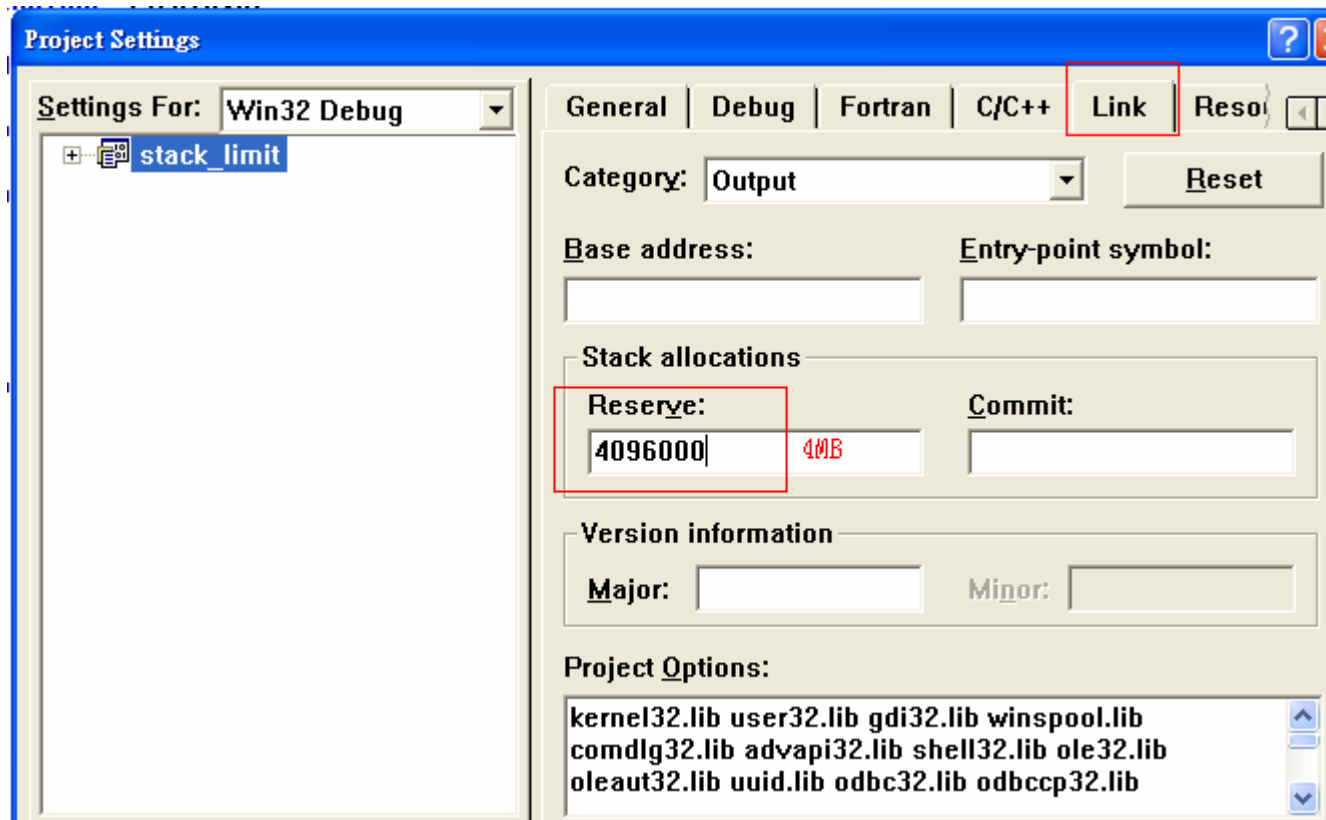
# modify stack limit in VC6.0

## /STACK (Stack Allocations)

[| Overview](#) | [| How Do I](#) | [| Linker Options](#)

The Stack Allocations (/STACK:reserve[,commit]) option sets the size of the stack in bytes.

To find this option in the development environment, click **Settings** on the **Project** menu. Then click the **Link** tab, and click Output in the Category box. The Reserve text box (or in the reserve argument on the command line) specifies the total stack allocation in virtual memory. The default stack size is 1 MB. The linker rounds up the specified value to the nearest 4 bytes.





# Exercise

- Write driver to test stack limit in VC6.0 and modify stack size in project setting dialog, does it work?
- Use the same driver, test stack limit on workstation with compiler g++ and icpc respectively. Is stack size independent of compiler?
- if we modify function *foo* such that local variable *word* is of no use what's stack size on workstation?

```
void foo( int level )
{
    char word[MAXBUFFER] ; // 1kB buffer in stack frame

    if ( 0 >= level ) { return ; }
    printf("level = %d\n", level);
    foo( level-1 ) ;
}
```

Local variable *word* is of no use.